

$\lambda$	$\rho_R$	$\alpha_\pi$	$\alpha_y$	$\alpha_{\Delta y}$	$\tau$	$\omega$
<i>Superinertial rule</i>						
0.25	1.2987	0.0313	0.0022	0.0166	0.3405	0.0491
1.1769	5	1.5372	0.0150	0.9426	0.0700	0.0196
$\infty$	5	4.1027	0.0000	0.0000	0.0000	0.4024
<i>Implementable rule</i>						
0.25	1	0.0595	0.0000	\	0.5590	0.0727
1.1769	1	0.1177	0.0000	\	0.2248	0.0857
$\infty$	1	0.4618	0.0000	\	0.0000	0.5945

Table 6: Robustness to alternative optimized monetary policy rule

becomes more mobile; ii) the welfare losses with respect to the Ramsey policy are smaller with respect to the price-level rules; iii) crucially, the negative relationship between labor mobility and the optimal weight on durables inflation survives.

We then replace rule (33) with an interest rate rule that responds only to inflation and the deviation of output from its steady state. Following Schmitt-Grohe and Uribe (2007) this type of interest rate rule is typically labelled *implementable rule* and, after the appropriate reparametrization, reads as follows:

$$\log\left(\frac{R_t}{\bar{R}}\right) = \rho_r \log\left(\frac{R_{t-1}}{\bar{R}}\right) + \alpha_\pi \log\left(\frac{\tilde{\Pi}_t}{\tilde{\Pi}}\right) + \alpha_y \log\left(\frac{Y_t}{\bar{Y}}\right), \quad (36)$$

where  $\alpha_\pi \equiv (1 - \rho_r) \rho_\pi$ ,  $\alpha_y \equiv (1 - \rho_r) \rho_y$ . The lower panel of Table 6 demonstrates that despite these modifications, the choice towards a price-level rule and the inverse relationship between labor mobility and the optimal weight on durables inflation still hold true. In addition, the implied welfare losses are similar to the baseline model.

## 5 Conclusion

As the New-Keynesian literature on two-sector models has demonstrated, setting the appropriate weights to sectoral inflations is a crucial task for a central bank in order to achieve its objectives. We look at this issue from an angle the literature has so far overlooked. In particular, we study the relation between the degree of sectoral

labor mobility and the optimal weight the central bank should assign to inflation in the sector with relatively more flexible prices (durables). We first estimate the model with Bayesian methods and find evidence of a limited sectoral labor mobility. Then, we exploit the estimated model to perform optimal monetary policy analysis. Under the Ramsey policy, the optimal responses to structural shocks are significantly altered by different degrees of sectoral labor mobility. Preventing labor from moving freely between sectors dramatically changes the optimal path of the policy rate, thus leading to different effects on sectoral and aggregate variables, as well as on welfare.

We then let the central bank optimize the parameters of a simple monetary policy rule along with the weight on inflation in the durables sector for different degrees of labor mobility. Our main result is that conditional on the intensity of price stickiness in the durables sector, an inverse relationship between labor mobility and the optimal weight on the sector with relatively more flexible prices arises: a lower weight is assigned to durables inflation as the degree of labor mobility increases. Intuitively, with more mobile labor, adjustments to shocks easily occur through quantities (via the reallocation of labor itself) rather than prices, and the central bank finds it optimal to focus more on the sector with the higher price stickiness.

Wage stickiness also plays an important role on the optimal weight of durables inflation. Via the pass-through on marginal costs it always implies a higher weight on durables inflation with respect to the case of flexible wages. In the design of optimal monetary policy, we also find that the central bank chooses to implement a price-level rule by introducing desirable history dependence in the model to reduce the volatility of prices, thus confirming results the literature has found in one-sector models.

These results are confirmed by various robustness checks and point to a non-negligible role of sectoral labor mobility for the conduct of monetary policy.

## References

- Aoki, K. (2001). Optimal monetary policy responses to relative-price changes. *Journal of Monetary Economics*, 48(1):55–80.
- Barsky, R. B., House, C. L., and Kimball, M. S. (2007). Sticky-price models and durable goods. *American Economic Review*, 97(3):984–998.
- Benigno, P. (2004). Optimal monetary policy in a currency area. *Journal of International Economics*, 63(2):293–320.

- Bils, M. and Klenow, P. J. (2004). Some evidence on the importance of sticky prices. *Journal of Political Economy*, 112(5):947–985.
- Bouakez, H., Cardia, E., and Ruge-Murcia, F. (2014). Sectoral price rigidity and aggregate dynamics. *European Economic Review*, 65(C):1–22.
- Bouakez, H., Cardia, E., and Ruge-Murcia, F. J. (2009). The transmission of monetary policy in a multisector economy. *International Economic Review*, 50(4):1243–1266.
- Bouakez, H., Cardia, E., and Ruge-Murcia, F. J. (2011). Durable goods, intersectoral linkages and monetary policy. *Journal of Economic Dynamics and Control*, 35(5):730–745.
- Cantelmo, A. and Melina, G. (2015). Monetary Policy and the Relative Price of Durable Goods. CESifo Working Paper Series 5328, CESifo Group Munich.
- Cantore, C., Levine, P., Melina, G., and Yang, B. (2012). A fiscal stimulus with deep habits and optimal monetary policy. *Economics Letters*, 117(1):348–353.
- Christiano, L. J., Eichenbaum, M., and Evans, C. L. (2005). Nominal rigidities and the dynamic effects of a shock to monetary policy. *Journal of Political Economy*, 113(1):1–45.
- Di Pace, F. and Hertweck, M. (2016). Labour market frictions, monetary policy and durable goods. Bank of England working papers 623, Bank of England.
- Erceg, C. and Levin, A. (2006). Optimal monetary policy with durable consumption goods. *Journal of Monetary Economics*, 53(7):1341–1359.
- Gerberding, C., Gerke, R., and Hammermann, F. (2012). Price-level targeting when there is price-level drift. *Journal of Macroeconomics*, 34(3):757–768.
- Giannoni, M. P. (2014). Optimal interest-rate rules and inflation stabilization versus price-level stabilization. *Journal of Economic Dynamics and Control*, 41(C):110–129.
- Giannoni, M. P. and Woodford, M. (2003). Optimal Interest-Rate Rules: I. General Theory. NBER Working Papers 9419, National Bureau of Economic Research, Inc.
- Horvath, M. (2000). Sectoral shocks and aggregate fluctuations. *Journal of Monetary Economics*, 45(1):69–106.
- Huang, K. X. and Liu, Z. (2005). Inflation targeting: What inflation rate to target? *Journal of Monetary Economics*, 52(8):1435–1462.
- Iacoviello, M. and Neri, S. (2010). Housing market spillovers: Evidence from an estimated DSGE model. *American Economic Journal: Macroeconomics*, 2(2):125–64.
- Jeske, K. and Liu, Z. (2013). Should The Central Bank Be Concerned About Housing Prices? *Macroeconomic Dynamics*, 17(01):29–53.

- Kara, E. (2010). Optimal monetary policy in the generalized Taylor economy. *Journal of Economic Dynamics and Control*, 34(10):2023–2037.
- Levine, P., McAdam, P., and Pearlman, J. (2008). Quantifying and sustaining welfare gains from monetary commitment. *Journal of Monetary Economics*, 55(7):1253–1276.
- Mankiw, N. G. and Reis, R. (2003). What Measure of Inflation Should a Central Bank Target? *Journal of the European Economic Association*, 1(5):1058–1086.
- Melina, G. and Villa, S. (2015). Leaning Against Windy Bank Lending. CESifo Working Paper Series 5317, CESifo Group Munich.
- Monacelli, T. (2008). Optimal monetary policy with collateralized household debt and borrowing constraints. In *Asset Prices and Monetary Policy*, NBER Chapters, pages 103–146. National Bureau of Economic Research, Inc.
- Monacelli, T. (2009). New Keynesian models, durable goods, and collateral constraints. *Journal of Monetary Economics*, 56(2):242–254.
- Nakamura, E. and Steinsson, J. (2008). Five facts about prices: A reevaluation of menu cost models. *The Quarterly Journal of Economics*, 123(4):1415–1464.
- Petrella, I., Rossi, R., and Santoro, E. (2016). Monetary policy with sectoral trade-offs. mimeo.
- Petrella, I. and Santoro, E. (2011). Input–output interactions and optimal monetary policy. *Journal of Economic Dynamics and Control, Elsevier*, 35(11):1817–1830.
- Rotemberg, J. J. (1982). Monopolistic price adjustment and aggregate output. *Review of Economic Studies*, 49(4):517–31.
- Schmitt-Grohe, S. and Uribe, M. (2007). Optimal simple and implementable monetary and fiscal rules. *Journal of Monetary Economics*, 54(6):1702–1725.
- Smets, F. and Wouters, R. (2007). Shocks and frictions in US business cycles: A Bayesian DSGE approach. *American Economic Review*, 97(3):586–606.
- Strum, B. E. (2009). Monetary Policy in a Forward-Looking Input-Output Economy. *Journal of Money, Credit and Banking*, 41(4):619–650.
- Woodford, M. (2003). *Interest and Prices. Foundations of a Theory of Monetary Policy*. Princeton University Press, Princeton, NJ.
- Zubairy, S. (2014). On fiscal multipliers: Estimates from a medium scale DSGE model. *International Economic Review*, 55:169–195.

# Appendix

## A Data

We define the durables sector as the a composite of durable goods and residential investments whereas the nondurables sector comprises nondurables goods and services.

Series	Definition	Source	Mnemonic
$DUR^N$	Nominal Durable Goods	BEA	Table 2.3.5 Line 3
$RI^N$	Nominal Residential Investment	BEA	Table 1.1.5 Line 13
$ND^N$	Nominal Nondurable Goods	BEA	Table 2.3.5 Line 8
$S^N$	Nominal Services	BEA	Table 2.3.5 Line 13
$P_{DUR}$	Price Deflator, Durable Goods	BEA	Table 1.1.9 Line 4
$P_{RI}$	Price Deflator, Residential Investment	BEA	Table 1.1.9 Line 13
$P_{ND}$	Price Deflator, Nondurable Goods	BEA	Table 1.1.9 Line 5
$P_S$	Price Deflator, Services	BEA	Table 1.1.9 Line 6
$Y^N$	Nominal GDP	BEA	Table 1.1.5 Line 1
$P_Y$	Price Deflator, GDP	BEA	Table 1.1.9 Line 1
$FFR$	Effective Federal Funds Rate	FRED	FEDFUNDS
$N$	Nonfarm Business Sector: Average Weekly Hours	FRED	PRS85006023
$W$	Nonfarm Business Sector: Compensation Per Hour	FRED	COMPNFB
$POP$	Civilian Non-institutional Population, over 16	FRED	CNP16OV
$CE$	Civilian Employment, 16 over	FRED	CE16OV

Table A.1: Data Sources

### A.1 Durables and Residential Investments

1. Sum nominal series:  $DUR^N + RI^N = DR^N$
2. Calculate sectoral weights of deflators:  $\omega^D = \frac{DUR^N}{DR^N}$ ;  $\omega^{RI} = \frac{RI^N}{DR^N}$
3. Calculate Deflator:  $P_D = \omega^D P_{DUR} + \omega^{RI} P_{RI}$

4. Calculate Real Durable Consumption:  $D = \frac{DUR^N + RI^N}{P_D}$

## A.2 Nondurables and Services

1. Sum nominal series:  $ND^N + S^N = NS^N$
2. Calculate sectoral weights of deflators:  $\omega^{ND} = \frac{ND^N}{NS^N}$ ;  $\omega^S = \frac{S^N}{NS^N}$
3. Calculate Deflator:  $P_C = \omega^{ND} P_{ND} + \omega^S P_S$
4. Calculate Real Nondurable Consumption:  $C = \frac{ND^N + S^N}{P_C}$

## A.3 Data transformation for Bayesian estimation

Variable	Description	Construction
$POP_{index}$	Population index	$\frac{POP}{POP_{2009:1}}$
$CE_{index}$	Employment index	$\frac{CE}{CE_{2009:1}}$
$Y^o$	Real per capita GDP	$\ln \left( \frac{Y^N}{POP_{index}} \right) 100$
$I_D^o$	Real per capita consumption: durables	$\ln \left( \frac{D}{POP_{index}} \right) 100$
$C^o$	Real per capita consumption: nondurables	$\ln \left( \frac{C}{POP_{index}} \right) 100$
$W^o$	Real wage	$\ln \left( \frac{W}{P_Y} \right) 100$
$N^o$	Hours worked per capita	$\ln \left( \frac{H \times CE_{index}}{POP_{index}} \right) 100$
$\Pi_C^o$	Inflation: nondurables sector	$\Delta (\ln P_C) 100$
$\Pi_D^o$	Inflation: durables sector	$\Delta (\ln P_D) 100$
$R^o$	Quarterly Federal Funds Rate	$\frac{FFR}{4}$

Table A.2: Data transformation - Observables

## B Symmetric equilibrium

$$X_t = Z_t^{1-\alpha} D_t^\alpha \quad (37)$$

$$Z_t = C_t - \zeta S_{t-1} \quad (38)$$

$$S_t = \rho_c S_{t-1} + (1 - \rho_c) C_t \quad (39)$$

$$U(X_t, N_t) = \log(X_t) - \nu \frac{N_t^{1+\varphi}}{1+\varphi} \quad (40)$$

$$U_{Z,t} = \frac{(1-\alpha)}{Z_t} \quad (41)$$

$$U_{D,t} = \frac{\alpha}{D_t} \quad (42)$$

$$U_{N,t} = -\nu N_t^\varphi \quad (43)$$

$$N_t = \left[ (\chi^C)^{-\frac{1}{\lambda}} (N_t^C)^{\frac{1+\lambda}{\lambda}} + (1 - \chi^C)^{-\frac{1}{\lambda}} (N_t^D)^{\frac{1+\lambda}{\lambda}} \right]^{\frac{\lambda}{1+\lambda}} \quad (44)$$

$$N_t^C = \chi^C \left( \frac{w_t^C}{w_t} \right)^\lambda N_t \quad (45)$$

$$N_t^D = \chi^D \left( \frac{w_t^D}{w_t} \right)^\lambda N_t \quad (46)$$

$$\Lambda_{t,t+1} \equiv \beta \frac{U_{Z,t+1} e_{t+1}^B}{U_{Z,t} e_t^B} \quad (47)$$

$$\begin{aligned} [1 - e_t^W \eta] + \frac{e_t^W \eta}{\tilde{\mu}_t} &= \vartheta^W (\Pi_t^W - \Pi^C) \Pi_t^W + \\ &+ E_t \left[ \Lambda_{t,t+1} \vartheta^W (\Pi_{t+1}^W - \Pi^C) \Pi_{t+1}^W \frac{w_{t+1} N_{t+1}}{w_t N_t} \right] \end{aligned} \quad (48)$$

$$\tilde{\mu}_t = -\frac{U_{Z,t}}{U_{N,t}} w_t \quad (49)$$

$$Q_t \psi_t = \frac{U_{D,t}}{U_{Z,t}} + (1 - \delta) E_t [\Lambda_{t,t+1} Q_{t+1} \psi_{t+1}] \quad (50)$$

$$\begin{aligned} 1 &= \psi_t e_t^I \left[ 1 - S \left( \frac{I_t^D}{I_{t-1}^D} \right) - S' \left( \frac{I_t^D}{I_{t-1}^D} \right) \frac{I_t^D}{I_{t-1}^D} \right] + \\ &+ E_t \left\{ \Lambda_{t,t+1} \psi_{t+1} \frac{Q_{t+1}}{Q_t} e_{t+1}^I \left[ S' \left( \frac{I_{t+1}^D}{I_t^D} \right) \left( \frac{I_{t+1}^D}{I_t^D} \right)^2 \right] \right\} \end{aligned} \quad (51)$$

$$S \left( \frac{I_t^D}{I_{t-1}^D} \right) = \frac{\phi}{2} \left( \frac{I_t^D}{I_{t-1}^D} - 1 \right)^2 \quad (52)$$

$$S' \left( \frac{I_t^D}{I_{t-1}^D} \right) = \phi \left( \frac{I_t^D}{I_{t-1}^D} - 1 \right) \quad (53)$$

$$1 = E_t \left[ \Lambda_{t,t+1} \frac{R_t}{\Pi_{t+1}^C} \right] \quad (54)$$

$$\Pi_t^D = \Pi_t^C \frac{Q_t}{Q_{t-1}} \quad (55)$$

$$\Pi_t^W = \frac{w_t}{w_{t-1}} \tilde{\Pi}_t \quad (56)$$

$$Y_t^C = e_t^A N_t^C \quad (57)$$

$$Y_t^D = e_t^A N_t^D \quad (58)$$

$$(1 - e_t^C \epsilon_c) + e_t^C \epsilon_c MC_t^C = \vartheta_c (\Pi_t^C - \Pi^C) \Pi_t^C - \vartheta_c E_t \left[ \Lambda_{t,t+1} \frac{Y_{t+1}^C}{Y_t^C} (\Pi_{t+1}^C - \Pi^C) \Pi_{t+1}^C \right] \quad (59)$$

$$MC_t^C = \frac{w_t}{e_t^A} \quad (60)$$

$$(1 - e_t^D \epsilon_d) + e_t^D \epsilon_d MC_t^D = \vartheta_d (\Pi_t^D - \Pi^D) \Pi_t^D - \vartheta_d E_t \left[ \Lambda_{t,t+1} \frac{Q_{t+1}}{Q_t} \frac{Y_{t+1}^D}{Y_t^D} (\Pi_{t+1}^D - \Pi^D) \Pi_{t+1}^D \right] \quad (61)$$

$$MC_t^D = \frac{w_t}{e_t^A Q_t} \quad (62)$$

$$\tilde{\Pi}_t = (\Pi_t^C)^{1-\tau} (\Pi_t^D)^\tau \quad (63)$$

$$\log \left( \frac{R_t}{\bar{R}} \right) = \left[ \rho_\pi \log \left( \frac{\Pi_t}{\bar{\Pi}} \right) + \rho_y \log \left( \frac{Y_t}{\bar{Y}} \right) \right] + e_t^M \quad (64)$$

$$Y_t^C = C_t + e_t^G + \frac{\vartheta_c}{2} (\Pi_t^C - \Pi^C)^2 Y_t^C \quad (65)$$

$$Y_t^D = [D_t - (1 - \delta) D_{t-1}] + \frac{\vartheta_d}{2} (\Pi_t^D - \Pi^D)^2 Y_t^D \quad (66)$$

$$Y_t = Y_t^C + Q_t Y_t^D + \frac{\vartheta^W}{2} (\Pi_t^W - \Pi^C)^2 w_t N_t \quad (67)$$



## C Steady state

In the deterministic steady state all expectation operators are removed and for each variable it holds that  $x_t = x_{t+1} = x$ . Moreover, the stochastic shocks are absent. The steady-state inflation rate in the nondurables sector is the optimal under the Ramsey policy and is denoted by  $\Pi_{\text{opt}}^C$ .  $C$  solves equation (65) whereas all other variables can be found recursively from the following relationships:

$$\Pi^D = \Pi_{\text{opt}}^C \quad (68)$$

$$\tilde{\Pi} = \Pi_{\text{opt}}^C \quad (69)$$

$$\Pi^W = \Pi_{\text{opt}}^C \quad (70)$$

$$\Lambda = \beta \quad (71)$$

$$R = \frac{1}{\beta} \quad (72)$$

$$MC_t^C = \frac{\epsilon_c - 1}{\epsilon_c} \quad (73)$$

$$w^C = MC^C e^A \quad (74)$$

$$w^D = w^C \quad (75)$$

$$w = w^D \quad (76)$$

$$MC_t^D = \frac{\epsilon_d - 1}{\epsilon_d} \quad (77)$$

$$Q = \frac{w^D}{MC^D e^A} \quad (78)$$

$$S = 0 \quad (79)$$

$$S' = 0 \quad (80)$$

$$\psi = 1 \quad (81)$$

$$\tilde{\mu} = \frac{\eta}{\eta - 1} \quad (82)$$

$$S = C \quad (83)$$

$$Z = (1 - \zeta) C \quad (84)$$

$$U_Z = \frac{(1 - \alpha)}{Z} \quad (85)$$

$$U_D = U_z Q \psi [1 - (1 - \delta) \beta] \quad (86)$$

$$D = \frac{\alpha}{U_D} \quad (87)$$