Monetary Policy Rules for Financially Vulnerable Economies

Eduardo Morón and Diego Winkelried
One distinguishable characteristic of emerging market economies is that they are not financially robust. These economies are incapable of smoothing out large external shocks, as sudden capital outflows imply large and abrupt swings in the real exchange rate. Using a small open-economy model, this paper examines alternative monetary policy rules for economies with different degrees of liability dollarization. The paper answers the question of how efficient it is to use inflation targeting under high liability dollarization. Our findings suggest that it might be optimal to follow a nonlinear policy rule that defends the real exchange rate in a financially vulnerable economy.

JEL Classification Numbers: E52, E58, F41
Keywords: Liability Dollarization, Inflation Targeting, Monetary Policy Rules, Latin America
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I. Introduction ......................................................................................................................... 3
II. An Overview of Monetary Policy in Latin America.......................................................... 8
III. A Small, Open-Economy Model.................................................................................. 11
   A. Supply, Demand, and Prices ..................................................................................... 11
   B. Risk Premium and Contractionary Depreciations ..................................................... 13
   C. The Central Bank, The Inflation Target, and the Optimal Policy............................. 17
IV. Model Parameterization ................................................................................................. 19
V. Model Solution and Simulations ..................................................................................... 21
   A. The Optimal Rule ...................................................................................................... 21
   B. Alternative Rules ....................................................................................................... 23
   C. On the Optimality of a (Nonlinear) Fear of Floating Rule ........................................ 24
VI. Conclusion ...................................................................................................................... 26

Text Tables
1. Volatility of Interest Rates and Exchange Rates............................................................... 6
2. Monetary and Exchange Rate Policy in Latin America in the 1990s................................. 9
3. Dollarization in Latin America ....................................................................................... 10
4. Financial Vulnerability in Latin America ........................................................................ 15
5. Model Dynamics Relationships of the Robust and Vulnerable Economies.................... 20
6. Baseline Parameters for Robust and Vulnerable Economies .......................................... 21
7. Optimal Rule for Robust and Vulnerable Economies .................................................... 22
8. Unconditional Standard Deviations Under the Optimal Rule ........................................ 22
9. Simple Fixed Rules for Robust and Vulnerable Economies .......................................... 23

Figures
1. Latin American Inflation Rate in the 1990s..................................................................... 8
2. Half-life of an Exchange Rate Shock for Perú and Uruguay, 10-year rolling sample...... 11
3. Dollarization and Financial Vulnerability in Latin America ........................................... 16
4. Variance Frontiers for Robust and Vulnerable Economies Under the Optimal Rule ....... 22
5. Comparing a Nonlinear Policy Rule and the Optimal Linear Policy in a Vulnerable Economy ...................................................................................................................... 26

Appendices
I. Data .................................................................................................................................. 28
II. The State Space Form of the Model .................................................................................. 29

Appendix Table I. SUR Models for Robust and Vulnerable Economies .............................. 30

References ............................................................................................................................. 31
I. INTRODUCTION

One offspring of the recent, yet recurring debate on the optimal exchange rate regime for emerging market economies is the so-called hollowing-out hypothesis. According to this, the choices are either a fully dollarized economy or a flexible exchange rate within an inflation-targeting (IT) framework. Those emerging market countries that do not favor the dollarization option face a shortened menu. The currency board option has been discarded, and Argentina is still trying to find a way out. The fixed exchange rate regime has been banned after the “Tequila crisis” episode in Mexico and the collapse of the Asian tigers. What are left are flexible exchange rate regimes.

In Latin America, Brazil, Chile, Colombia, and, recently, Mexico have adopted flexible regimes but with a different flavor. All of them have IT schemes, meaning flexible exchange rates with a strong commitment that the inflation rate will not exceed (or fall below) a certain target undertaken. Along with that pack of countries, Perú and Uruguay are discussing and/or preparing the formal adoption of a similar framework.

The crucial difference between this group of countries (Latin American inflation targeters) and Perú and Uruguay is that the former are not heavily dollarized. The main question of the paper is what are the consequences of adopting an IT framework in economies that are liability dollarized as having a fully flexible exchange rate regime might imply a large balance sheet problem. We will focus on evaluating alternative monetary policy rules that might be implemented within this framework rather than comparing the IT option with other possibilities.

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2 The hollowing-out hypothesis is tested using different methodologies in Frankel and others (2000) and Masson (2000). Williamson (2000) argues against this hypothesis and defends the intermediate regimes for emerging economies. Velasco (2000) also supports the idea that the corners are not the best options to follow.

3 The LACEA 2000 meeting was a good example of this. Stanley Fischer at the inaugural lecture defended the flexible option and Rudi Dornbusch closed the event advising to switch to a fully dollarized regime. Mishkin and Savastano (2000) discuss, within the context of Latin America, which is the optimal monetary policy emphasizing the idea that the focus should be on the monetary policy and not on the exchange rate regime.

4 See Morandé and Schmidt-Hebbel (2000) for Chile, Bogdansky and others (2001) for Brazil and Martínez and others (2001) for México.

5 There are no good measures of financial vulnerabilities for emerging markets. This is an area in which more effort should be put as what matters is the net position of asset and liabilities of each particular sector: banks, firms, households, and government. Aggregate positions might be hiding large sectoral imbalances.

6 Masson, and others (1997) discusses the more general case for developing countries in general and found that Chile, Colombia and Mexico were good candidates to implement IT. As mentioned, all three are now following an IT framework.

7 Céspedes and others, (2000), Ghironi and Rebucci (2000) focus more on evaluating the alternative options of fixed, flex, currency board or full dollarization.
Masson and others (1997) suggest that economies should satisfy at least two prerequisites if they wish to consider the possibility of adopting IT: first, the ability to conduct independent monetary policy and, second, the ability to develop a quantitative framework linking policy instrument to inflation. The second requirement is not very restrictive, as the Brazilian case has shown how fast an economy can implement it. However, the first requirement encompasses a non-fiscal dominance condition and the absence of commitments to another nominal anchor. Most emerging market economies cannot satisfy entirely such conditions. However, it is hard to argue that fiscal dominance is a key factor only in the case of an IT regime. Even a fully dollarized economy that lacks fiscal sustainability will be severely hit when shocks come. Of course, it will make a lot of sense to reinforce the fiscal stance in all emerging market economies no matter what monetary or exchange rate policy are currently following. In terms of our discussion on the optimality of alternative policy rules, we will assume that the government not only engages in a fully credible way in the IT framework but also takes the necessary steps to avoid fiscal dominance. Also, we are not comparing the transition period of an IT regime but the behavior of that regime when we are in a new steady state.

As stressed by Calvo (2000) a remarkable difference between emerging market and developed economies lies in the importance of the structure of liabilities and the relationship between exchange rate regimes and financial fragility. Together with Mishkin (2000), he argues that a high degree of liability dollarization may hinder the feasibility of adopting an IT. As real exchange depreciations might trigger financial crisis, the exchange rate might become another target for the central bank. This will induce a larger problem as firms and households will expect that the implicit insurance against exchange rate risk will be maintained especially in turbulent times.

Another reason might be a concern for the exchange rate pass-through on inflation. Latin American countries have been known for their high inflations in the past. The recent trend of low inflation is something relatively new. In a “truly” flexible exchange rate regime, the exchange rate is supposed to work as an external shock absorber but we are considering rather extreme cases. If the economy has a high degree of pass-through, bad past memories might kick in and inflation will go up, as the real exchange rate is a forward-looking variable. Contrary to the common wisdom, pass-through estimates are now very low in both Perú and Uruguay (see section 2 below). However, the data seems to support the hypothesis that the pass-through is regime-dependent hence, the current low estimates should be taken with caution.

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8 See Bogdanski and others (2000) for an account of the process of implementing the IT framework in Brazil.
9 Most of the central banks in the region had improved their independence and autonomy with stricter charters that aim to avoid fiscal dominance.
11 See González (2000) for an estimation of the degree of exchange rate pass-through in a group of Latin American economies.
Perhaps the most striking distinction between the emerging markets and the developed ones is the fact that the former are incapable of smoothing out sudden changes in their external financing needs.\textsuperscript{13} Calvo (2000) has argued that those Latin American countries with highly dollarized liabilities will be more exposed to these perils. As nobody could argue that a market-based de-dollarization is feasible in the short or medium-term, we should treat that constraint as a permanent one.

A much more important constraint is that in economies with high levels of liability dollarization, the balance sheet channel dominates the more traditional interest rate channel on aggregate demand. The data shows (see Table 1) that as we move towards a more fixed regime, interest rates will be more volatile compared to exchange rates suggesting that is much more costly to freely float than to allow interest rate hikes. Lahiri and Végah (2001) shows that this policy could be rationalized as optimal in the context of a model in which real exchange rate fluctuations are costly.

Notwithstanding all of the above, Perú and (to a lesser extent) Uruguay are considering the pros and cons of adopting an IT framework.\textsuperscript{14} Both countries have curbed inflation to one-digit levels after a severe and chronic inflationary history and are among the group of the more dollarized economies in the region and therefore are forced to fear a sudden real depreciation because of the problems that a liability-dollarized economy might pose to a vulnerable financial system.\textsuperscript{15} This raises the obvious question of how feasible it is to have an IT regime in that type of economy.

Despite all these restrictions, these two countries and probably others (for example, Turkey) will join the bandwagon and adopt IT strategies to direct their monetary policies.\textsuperscript{16} What will be the consequences of following this option in terms of real exchange rate volatility, output, and inflation? The trade-off of having a wider inflation target band with an implicit narrow real exchange rate band calls into question the credibility of the inflation target. However, a wider real exchange rate band might call into question the sustainability of the regime, as the real consequences might be widespread bankruptcies and output instability.

\textsuperscript{13} For example, Argentina was put out of the market before the blindaje, and Perú suffered a severe cut of all banking credit lines after the Russian crisis.

\textsuperscript{14} See Licandro (2001) for a discussion of the Uruguayan case, and Armas et.al. (2001) for the Peruvian case.

\textsuperscript{15} Castro and Morón (2000) argued that the Peruvian Central Bank was unable in the 90s to use the flexible exchange rate regime as an external shock absorber due to the presence of a high degree of liability dollarization. See Calvo and Reinhart (2000) for a much broader perspective on the issue of liability dollarization, and Tornell (2000) for a model that describes this issue.

\textsuperscript{16} Eichengreen and others (1999) discuss IT as an exit strategy for previously fixed exchange rate regimes. However, both in Perú and Uruguay the reason behind the adoption of an IT framework is to consolidate the one-digit inflation rate obtained after a long lasting stabilization program, and keep the credibility gained after that effort.
Table 1. Volatility of Interest Rate and Exchange Rate

<table>
<thead>
<tr>
<th>Type of exchange Rate Regime</th>
<th>Probability that the monthly change in nominal exchange rate falls within:</th>
<th>Probability that the monthly change in nominal interest rate falls within:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>+/- 1.0% band</td>
<td>+/- 2.5% band</td>
</tr>
<tr>
<td>Floating</td>
<td>51.7</td>
<td>79.3</td>
</tr>
<tr>
<td>Managed floating</td>
<td>60.1</td>
<td>87.5</td>
</tr>
<tr>
<td>Limited flexibility</td>
<td>64.6</td>
<td>92.0</td>
</tr>
<tr>
<td>Fixed</td>
<td>83.1</td>
<td>95.9</td>
</tr>
</tbody>
</table>

Memo:
United States: 26.8, 58.7, 59.7, 80.7
Japan: 33.8, 61.2, 67.9, 86.4
Perú: 45.2, 71.4, 24.8, 32.3
Uruguay: 22.7, 92.0, 2.7, 8.0

Source: Calvo and Reinhart (2000)
Note: “bps” denotes basis points.

Even though the recommendation regarding avoiding mixing inflation targeting with exchange rate targeting seems completely necessary, it’s hard to draw a precise line in theory (or in practice) between when to lean against the wind and when to let the wind blow.\footnote{See Kumhoff (2000) on this. See also Mishkin (2000).} As stressed by Mishkin and Savastano (2000), letting the exchange rate become the \textit{de facto} nominal anchor of the economy through excessive intervention in a quasi-inflation targeting regime is an example of bad monetary policy under flexible exchange rates.\footnote{A very recent example of this is the mounting pressure on the Central Bank of Brazil officials to intervene in the foreign exchange market after the recent crisis in Argentina.}

In a recent policy note Perry (2001) considers that is too difficult whether to suggest to this type of country that they follow the full-dollarization option or the IT strategy. As we said before, we are not aiming to answer such a broad question. The goal of the paper is much more limited. If we take for granted that these two countries will move to an IT, which monetary policy rules should be considered the closest cousins of optimal rules? Some of the questions that we will try to answers are (i) should the central bank consider the exchange rate within its monetary policy rule? (ii) what are the consequences of a higher level of activism with respect to the exchange rate? (iii) what are the trade-offs involved in adopting a stricter or a more flexible IT regime?

Prior to the Asian crisis, only a very scant literature discussed the optimality of adopting IT for emerging markets. Most of the IT literature was focused on developed economies. Only very recently, has the literature on IT become much more concerned with developing models for small, open economies.\footnote{See Ball (1999), Clarida and others (2001) and Svensson (2000). They are just a few of many recent papers in this strand of the literature.} The survey by Mishkin and Savastano (2000) or the work of Frenkel (1999) showed that much more analytical work needs to be...
done to understand the real benefits from a regime that has not been tried in a partially dollarized environment. Taylor (2000) suggests that models like those in Svensson (2000) or Battini and others (2001) should be adjusted for the emerging markets to reflect the fact that exchange rate fluctuations are more costly there than in developed economies owing to the presence of currency and maturity mismatches.

Fortunately, the literature on monetary policy rules for emerging economies has been expanding very fast in the last year. Among the most important contributors are the following papers: Céspedes and others (2000) argue that in a model in which balance sheet effects *a la* Bernanke and Gertler (1989) matter, the horse race is won by the flexible exchange rate regime. They show that the contractionary effect of real exchange rate depreciation through that channel will be offset by effects transmitted by other channels (i.e. net worth, risk premium, real wages, and external debt). Therefore flexible exchange rate regimes maintain their superiority as shock absorbers compared with the fixed exchange regimes.

Gertler and others (2001) provide a comprehensive comparison of fixed versus flexible exchange rate regimes. Perhaps the most important result is that the welfare challenge could go either way depending on the extent to which the market value of domestic assets is used to collateralize lending. As the authors suggest, if capital markets are shallow, as in some emerging markets, a fixed exchange rate regime case is much stronger than a flexible exchange regime in the presence of foreign currency debt and a financial accelerator.

Devereux and Lane (2000), following Bernanke and others (2000), specify and calibrate a two-sector model using data for Thailand. They conclude that when constraints in external financing become more important, the benefits associated with monetary policy rules that include the real exchange rate become smaller. The paper’s weakness is that the IT rules are simple Taylor rules and not inflation forecast-based (IFB) rules. In the same way, Cook (2000) calibrates -using data for Southeast Asia- a model in which the entrepreneurs may borrow only in foreign currency and compares it with another model in which there is no liability dollarization. His main findings are that a fixed exchange rate regime is better, in terms of welfare, than a simple IT rule. However, these results assume that agents do not hedge against the exchange rate risk even though they are fully liability dollarized.

In a similar fashion, Ghironi and Rebucci (2000) use Argentina as an example to compare, in terms of welfare, three alternative regimes: a currency board, a full-dollarization regime, and an IT framework. The ranking of these three options depends heavily on the relationship between currency and default risk, which is not included in the model.20

In this paper, we consider a model that borrows the structure of Svensson (2000) and includes an explicit role for balance sheet effects as in Céspedes and others (2000) and Bernanke and others (2000). We calibrate the model for a financially robust economy and a

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20 Druck and others (2001) showed that the sign of the correlation of those risks depend on the presence (or not) of balance sheet effects in the economy.
financially vulnerable economy. For the former, we use Australian and New Zealand data, and for the latter we use Peruvian and Uruguayan data.

The structure of the paper is as follows. Section II briefly describes the different monetary policy choices made in Latin America in the past decade. Section III presents a small, open-economy model that will describe the transmission channels and discuss which ones are more important. Section IV presents the model parameterization. Section V discusses the optimality of alternative policy rules for both the financially vulnerable and financially robust economy cases. In addition, we study the optimality of nonlinear policy in the vulnerable economy case. In Section VI we conclude and discuss new avenues for further research.

II. AN OVERVIEW OF MONETARY POLICY IN LATIN AMERICA

The long-term quest for one digit inflation is about to become a reality for all Latin American countries. After three decades of high inflation the region has come back on track and the downward trend on inflation looks very promising (see Figure 1).21

Figure 1. Latin American Inflation Rate in the 1990s (logarithmic scale)

A key feature of this recent disinflation is that even though the outcome is more or less homogeneous across the board, the policies used have been quite disparate. Table 2 shows that a variety of nominal anchors and exchange rate regimes have been used. Just to add to the differences, Ecuador and El Salvador dollarized their economies while others are moving toward the recent trend of setting inflation targets as a framework for monetary

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21 The only exceptions are Ecuador and Venezuela. Ecuador fully dollarized its economy at the beginning of 2000 and the inflation rate for 2001 was 22.4 percent, while in Venezuela was 12.3 percent.
policy (Mexico, Perú). However, Latin America has not been the exception in the worldwide trend toward more flexible exchange rates.

Table 2. Monetary and Exchange Rate Policy in Latin America in the 1990s

<table>
<thead>
<tr>
<th></th>
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<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Argentina</td>
<td>e</td>
<td>Yes</td>
<td>1991</td>
<td>Fixed</td>
<td>1343.9</td>
<td>-0.7</td>
</tr>
<tr>
<td>Bolivia</td>
<td>m</td>
<td>No</td>
<td>1995</td>
<td>Managed-Bands</td>
<td>18.0</td>
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</tr>
<tr>
<td>Brasil</td>
<td>π</td>
<td>Yes</td>
<td>1999</td>
<td>Managed-Floating</td>
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<tr>
<td>Chile</td>
<td>π</td>
<td>Yes</td>
<td>1989–99</td>
<td>Floating</td>
<td>27.3</td>
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</tr>
<tr>
<td>Colombia</td>
<td>π</td>
<td>Yes</td>
<td>1991–99</td>
<td>Bands-Floating</td>
<td>32.4</td>
<td>8.8</td>
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<tr>
<td>Costa Rica</td>
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<td>10.4</td>
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<tr>
<td>Ecuador</td>
<td>$</td>
<td>Yes</td>
<td>1992–2000</td>
<td>Managed-Fixed</td>
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<td>96.6</td>
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<tr>
<td>El Salvador</td>
<td>$</td>
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<td>Managed-Bands</td>
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<td>Floating-Managed</td>
<td>59.6</td>
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<td>Mexico</td>
<td>π</td>
<td>In transition</td>
<td>1995–2001</td>
<td>Managed-Floating</td>
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<td>Managed-Floating</td>
<td>44.1</td>
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<td>Perú</td>
<td>π</td>
<td>In transition</td>
<td>1994</td>
<td>Managed-Floating</td>
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<td>Uruguay</td>
<td>e</td>
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<td>1995</td>
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<td>Venezuela</td>
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<td>1992</td>
<td>Fixed (Bands)-Floating</td>
<td>36.5</td>
<td>14.2</td>
</tr>
</tbody>
</table>

Notes: The first three columns are based on Corbo (2000), Mishkin and Savastano (2000), and several central bank reports. The third column refers to years in which there has been a substantial reform in the Charter of the central bank or the startup of target announcements. The fourth column might show two regimes as some transition has happened. The fifth column is the annual variation of CPI, according to World Bank reports.

Another key characteristic of Latin America is a by-product of the high-inflation experience. In Table 3 we show a raw measure of liability dollarization. The differences are quite marked across the countries. This combination (liability dollarization and flexible exchange rates) does not seem to be the best one. Berg and Borensztein (2000) suggest that highly liability dollarized economies should move toward a more fixed regime (full dollarization) whereas the rest of the economies should choose a more flexible exchange

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22 However, there is still work to do with respect to central bank independence, operational transparency and accountability. For further discussion see Mishkin and Savastano (2000) and Mishkin (2000).

23 Another caveat is the real meaning of fixed and flexible when we discuss exchange rate regimes. As Calvo and Reinhart (2000) and Levy and Sturzenegger (2000) have pointed out, there is a big gap between what countries say about their exchange rate regimes and what they actually do. In Table 2 we use Levy and Sturzenegger (2000) classification index to take into account these considerations.
rate regime. As discussed by Calvo and Végh (1996), the distinction between currency and asset (liability) substitution is crucial. The macroeconomic instability of Latin American economies linked to real exchange rate fluctuations is not related to the standard argument that it is impossible to pursue an independent monetary policy when currency substitution is widespread. The macroeconomic fluctuations are mostly the consequence of the effects of real exchange rate fluctuations on a banking system and, through it, in firms and households in which liabilities have been heavily dollarized.

Table 3. Dollarization in Latin America

<table>
<thead>
<tr>
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<td>Argentina</td>
<td>43.85</td>
<td>44.81</td>
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<td>Bolivia</td>
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<td>81.12</td>
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<td>10.46</td>
<td>13.14</td>
<td>2.56</td>
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<td>28.05</td>
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<td>41.02</td>
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<td>El Salvador</td>
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<td>-11.57</td>
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<td>83.98</td>
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</tbody>
</table>

Notes: The figures correspond to the ratio of dollar deposits in the banking system to M3. All data is from the World Bank except for Argentina, Colombia, Guatemala and Uruguay, for which the data comes from their central banks. We could not find data for Brazil and Venezuela.

It is not clear what the optimal choice of monetary and exchange rate policy should be if an economy is liability dollarized. Much of the earlier literature focused on only the currency-substitution case in which the choice is much easier. However, that is no longer the most critical problem. The low-inflation period that the region has enjoyed has restored much weight to the domestic currency in the typical transactions motive for holding money across countries. So, it seems that the hysteresis hypothesis is valid in the asset and liability dollarization but not in the currency-substitution process.

Another pain in the neck for those emerging market economies that wish to have a floating exchange rate cum inflation targeting is the pass-through coefficient from the

24 Calvo (1999) and Hausmann and others (1999) are also in the same line.

25 Morón (1997) test the Calvo and Végh (1996) hypothesis for Perú and found a very distinguishable behavior for estimated currency substitution and asset substitution ratios based in a Divisia-type model.

26 If an economy faces nominal (real) shocks more often than real (nominal) shocks, the optimal regime is a fixed (flexible) exchange rate. See Mundell (1961).
exchange rate to domestic prices. We calculate 10-year rolling estimates of this coefficient for Perú and Uruguay. The results are shown in Figure 2. Surprisingly, the half-life of an exchange rate shock increased substantially in the 1990s. This could be interpreted as a significant reduction in the inflationary inertia after successful disinflation programs or as an improvement in the credibility of the central banks. These results go against the conventional wisdom that emergent economies that have experienced high and recurrent inflation periods should be characterized as economies with high pass-through coefficients.

Figure 2. Half-life of an Exchange Rate Shock for Perú and Uruguay, 10-Year Rolling Sample (months)

III. A SMALL, OPEN-ECONOMY MODEL

Based on the previous work of Ball (1999), Leitemo (1999), and specially Svensson (2000) on open economies, we propose a small, open-economy model that will help us to derive quantitative results about the transmission mechanisms that underlie a liability-dollarized economy and to discuss the policy options in such an economy. The model is a standard forward-looking, rational-expectations model, in which the monetary authority has a flexible exchange rate regime and cares about inflation and output variability. We explicitly include the financial-vulnerability characteristic as in Bernanke and others (1998) and Céspedes and others (2000).

We want to answer the question of what is the optimal way to implement monetary policy for a given set of economic characteristics as discussed in Poole (1970). In our case, the defining characteristic would be the financial robustness or weakness of the economy.

A. Supply, Demand, and Prices

All variables except the interest rate are in logs and measured as deviations from their long run equilibrium level, in order to work with a stationary system. We use the notation $z_{t+k|t}$ for the rational expectation of $z_{t+k}$ with all the information available at $t$.

27 We followed Gonzales (2000) methodology but used 10-year rolling samples.
The short run supply curve, the Phillips Curve, of the economy could be written as\(^{28}\)

\[
\pi_{t+2} = \alpha_{\pi} \pi_{t+1} + (1 - \alpha_{\pi}) \pi_{t+3/4} + \alpha_y y_{t+1/4} + \alpha_q q_{t+2/4} + \epsilon_{t+2}
\]  

(1)

where \(\pi_t\) is the domestic inflation at period \(t\), a predetermined variable two periods ahead, while \(y_t\) is the output gap. All coefficients of (1) are positive constants (\(\alpha_{\pi}\) is less than one) and the term \(\epsilon_{t+2}\) represent zero mean i.i.d. cost push shock.

The real exchange rate, \(q_t\), is defined by

\[
q_t = s_t + p_t^* - p_t
\]

(2)

where \(p_t\) is the domestic price level, \(p_t^*\) is the foreign price level and \(s_t\) denotes the nominal exchange rate. On the other hand, aggregate demand could be expressed\(^{29}\)

\[
y_{t+1} = \beta_x y_t - \beta_r r_{t+1/4} + \beta_q q_{t+1/4} + \beta_p^* p_{t+1/4} - \beta_p^* \varphi_{t+1/4} + \eta_{t+1}
\]

(3)

where \(y_t^*\) is the foreign demand and \(\varphi_t\) is the risk premium, which will be a crucial variable on the following analysis. All coefficients in (3) are positive and \(\eta_{t+1}\) represents a zero mean i.i.d. demand shock. The Fisher equation holds,

\[
r_t = i_t - \pi_{t+1/4}
\]

(4)

and define \(r_t\), as the short term real interest rate (\(i_t\) is the short term nominal interest rate). The nominal exchange rate satisfy the uncovered interest parity condition,

\[
i_t - i_t^* = s_{t+1/4} - s_t + \varphi_t
\]

(5)

where \(i_t^*\) is the foreign interest rate. Using (2) and (5) the real interest parity condition is obtained,

\[
q_{t+1/4} = q_t + i_t - \pi_{t+1/4} - i_t^* + \pi_{t+1/4}^* - \varphi_t
\]

(6)

Finally, we assume that foreign output, inflation and interest rate are all exogenous. To keep things simple, the first two follow a first-order autoregressive process, while the third one is determined by a Taylor rule:

\[
\pi_{t+1}^* = \gamma_{\pi} \pi_t + \epsilon_{t+1}
\]

(7)

---

\(^{28}\) In a Calvo price-setting framework, the typical aggregate supply curve from the intertemporal maximization of a representative agent that demands domestic and foreign goods is

\[
\pi_t = \theta \pi_{t+1/4} + \omega_y y_t + \omega_q q_t
\]

In order to enrich the model dynamics, it is imposed a partial adjustment mechanism and it’s also considered a two-period ahead predetermined inflation.

\(^{29}\) A micro founded derivation of a similar aggregate demand curve is available in Svensson (2000).
where coefficients are positive ($\gamma_{x}$ and $\gamma_{y}$ are less than one) and disturbances are i.i.d.

\[ y_{t+1}^* = \gamma_{x} y_{t}^* + \eta_{t+1}^* \]  
\[ i_{t}^* = f_{t}^* \pi_{t}^* + f_{y} y_{t}^* + \xi_{t}^* \]

\[ (8) \]
\[ (9) \]

**B. Risk Premium and Contractionary Depreciations**

In a general equilibrium setting under price rigidities, the risk premium comes from the correlation between household consumption and the exchange rate. Instead of assuming the risk premium as an exogenous process, as in many studies, we link its behavior with the net worth of entrepreneurs that are liability dollarized.

An attempt to endogenize the risk premium within a closed economy with asymmetric information and principal-agent problems is presented by Bernanke and others (2000). They rely on the premise that the deterioration of domestic credit market conditions not only reflects problems at the real side of the economy, but also there are frictions that might constitute the main depressing factor of economic activity. In other words the credit market works as an amplifier of both nominal and real shocks as in Kiyotaki and Moore (1997). The core of this mechanism, known as the *financial accelerator*, consists of an inverse relation between the external finance premium and the net worth of potential borrowers. The external finance premium is defined as the difference between the cost of external funds and the opportunity cost of firms to finance their operations with internal resources. The net worth of borrowers is the value of their liquid assets (internal funds) plus the collateral value of their illiquid assets minus non-performing liabilities. Under an underdeveloped domestic financial market and when creditors have limited resources to finance investment projects, the equilibrium implies that lenders will have to be compensated with a larger financial risk premium.

Céspedes and others (2000) and Gertler and others (2001) extend the previous analysis to an open economy framework in which firms demand dollar-denominated foreign loans and the external finance premium may be thought as an exchange rate risk premium. These authors model the links between the real exchange rate, the net worth of firms and the risk premium, focusing on balance sheet effects and taking as a starting point the budget constraint of firms that engage in investment. Considering that the risk premium is an inverse function of the value of the firms' net worth and as the cost of external financing comes as given by the foreign interest rate plus the risk premium, Céspedes and others (2000), determine that the evolution of the risk premium follows:

\[ \varphi_{t+1} - \varphi_{t} = -\psi_{2} x_{t} + \psi_{2} (y_{t} - q_{1}) - \psi_{3} [(y_{t} - y_{t/t-1}) - (q_{1} - q_{t/t-1})] \]

where all coefficients are positive constants. The change in the risk premium depends on three factors. The first term is related with changes in the demand for exports, denoted as $x_{t}$; given an output level, a rise in exports is compensated by a lower investment that requires less external financing and therefore a lower risk premium. The second term

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30 See Chang and Velasco (2000). See also footnote 19.
captures the effects of changes in output and the real exchange rate, or in real output valued in dollars. A decrease in \( y_t - q_t \) (either due a lower \( y_t \) or a higher \( q_t \)) implies lower levels of investment and again lower financing needs and lower risk premium. Finally, the third term represents the unexpected changes in output measured in dollars, closely linked to firms’ net worth. An unanticipated real depreciation increases the burden of the debt (denominated in dollars) that lowers the firms’ net worth.

A higher real exchange rate increases the cost of investment relative to firms’ net worth. Moreover, lower output levels will reduce the return of previous realized investments. In that sense, a real depreciation or a decline in output might generate positive effects over the risk premium.\(^{31}\)

Assuming that exports are a linear function of foreign demand and the risk premium is subject to \( i.i.d. \) disturbances \( \xi_{p,t} \), equation (10) could be written as

\[
\varphi_{t+1} = \varphi_t - \psi_1 y_t^* + (\psi_2 - \psi_3)(y_t - q_t) + \psi_3(y_{t/t-1} - q_{t/t-1}) + \xi_{p,t+1}
\]  

(11)

As in Cespedes and others (2000) we distinguish two types of economies regarding the impact that balance sheet effects might have. A financially robust economy is one in which the transmission channel of a real exchange rate depreciation to output is dominated by the price effect predicted in the textbook case of open economies. A real depreciation increases output in the short run as the external competitiveness of the economy improves. In the other hand, in a financially vulnerable economy the depreciation is contractionary, basically due to the dominance of the negative wealth effect over the price effect above mentioned. A real depreciation increases the competitiveness of the economy but at the same time reduces the net worth of firms, as they are liability dollarized.

Using equation (11), the elasticity of the risk premium to the real exchange rate is given by:

\[
\frac{\partial (\varphi_{t+1} - \varphi_t)}{\partial q_t} = \psi_3 - \psi_2 = \lambda
\]  

(12)

In a financially vulnerable economy \( \lambda \) is positive while in a robust one, \( \lambda \) is negative so the direct comparison of the values of \( \psi_2 \) and \( \psi_3 \) characterize the financial vulnerability. Consequently, there is a mechanism by which the potential positive effect of a real depreciation over the risk premium generates, by the interest parity condition, a higher local interest rate and therefore a recession. Likewise, Hausmann and others (2000) suggest that, in a liability dollarized economy with incomplete pass-through, the exchange rate fluctuations have an impact on output via two channels, a direct wealth effect (the balance

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\(^{31}\) Powell and Sturzenegger (2000) use an event study approach to test the relationship between financial fragility and country risk. Excepting Chile and Colombia, the authors find that the country risk will reduce significantly if countries (Argentina, Brazil, Ecuador and Mexico) dollarize.
sheet channel) and a credit channel through an increase in the interest rate. If the first one dominates the second, the depreciation will be contractionary.32

Céspedes and others (2000) find that the steady state value of $\lambda$ is proportional to the ratio dollar-debt to investment (see the first three columns of Table 4). A higher dollar debt-to-capital ratio will imply that $\lambda$ is nonnegative and therefore the economy is more vulnerable.

Table 4. Financial Vulnerability in Latin America

<table>
<thead>
<tr>
<th>Country</th>
<th>NPV of Debt to Investment Ratio</th>
<th>GDP Services (% of GDP)</th>
<th>Elasticity of Risk Premium to Real Exchange Rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bolivia</td>
<td>3.10 3.92</td>
<td>2.51 0.43</td>
<td>62.4 63.5 0.2497 (0.1704)</td>
</tr>
<tr>
<td>Brazil</td>
<td>1.38 1.33</td>
<td>1.31 0.38</td>
<td>62.8 59.9 0.3349 (0.0314)*</td>
</tr>
<tr>
<td>Chile</td>
<td>1.64 2.59</td>
<td>1.96 1.35</td>
<td>57.4 57.4 -0.2105 (0.1638)</td>
</tr>
<tr>
<td>Colombia</td>
<td>1.72 3.07</td>
<td>1.68 1.09</td>
<td>61.0 62.9 -0.0492 (0.0210)**</td>
</tr>
<tr>
<td>Costa Rica</td>
<td>1.40 1.68</td>
<td>1.33 0.55</td>
<td>56.7 56.8 -0.1044 (0.0402)*</td>
</tr>
<tr>
<td>Ecuador</td>
<td>3.11 6.57</td>
<td>2.92 3.45</td>
<td>55.2 50.3 -0.0523 (0.0817)</td>
</tr>
<tr>
<td>El Salvador</td>
<td>1.74 1.85</td>
<td>1.55 0.19</td>
<td>60.4 60.0 -0.0979 (0.0371)*</td>
</tr>
<tr>
<td>Guatemala</td>
<td>1.31 1.44</td>
<td>1.41 0.20</td>
<td>56.6 56.8 -0.0897 (0.0257)*</td>
</tr>
<tr>
<td>México</td>
<td>1.58 1.47</td>
<td>1.54 0.95</td>
<td>66.3 66.8 0.1726 (0.0605)*</td>
</tr>
<tr>
<td>Nicaragua</td>
<td>8.40 6.63</td>
<td>7.38 0.42</td>
<td>45.4 45.7 0.0110 (0.0048)**</td>
</tr>
<tr>
<td>Paraguay</td>
<td>1.17 1.65</td>
<td>1.10 0.06</td>
<td>48.8 46.1 -0.2323 (0.1348)</td>
</tr>
<tr>
<td>Perú</td>
<td>2.12 2.62</td>
<td>2.20 0.67</td>
<td>56.1 55.5 -0.1244 (0.0545)**</td>
</tr>
<tr>
<td>Uruguay</td>
<td>3.87 4.13</td>
<td>2.08 1.02</td>
<td>65.3 68.0 0.2136 (0.0462)*</td>
</tr>
<tr>
<td>Venezuela</td>
<td>1.83 2.33</td>
<td>1.86 1.73</td>
<td>59.6 68.5 0.2517 (0.1248)**</td>
</tr>
</tbody>
</table>

Memo:

- Australia: -0.0994 (0.0377)*
- New Zealand: -0.1082 (0.0406)*

Notes: The term “Debt” refers to “External Debt”. Columns 1 to 4 correspond to World Bank figures. In column 5 we show estimates of equation (11) with monthly data from the IMF, from January 1991 to December 2000 (see Appendix B2 for further details), except Peru and Costa Rica (from January 1992 to December 2000) and Brazil (from January 1994 to December 2000). Figures in parenthesis are standard errors of estimated coefficients. * denotes statistical significance at 5 percent and ** at 10 percent.

An alternative approach is suggested by Calvo and Reinhart (2000) with emphasis on the degree of capital mobility. The approach is motivated by depreciations in emerging economies that have suffered from sudden stops in the access to external funding as in Brazil in 1999. Under imperfect capital mobility, there are real balance restrictions that

32 Faced with a negative external shock the central bank will tighten the monetary policy (i.e. increasing the interest rate) that will partially offset the exchange rate depreciation. According to Hausmann and others (2000), the monetary authority will respond to both nominal and real shocks. In an extreme case, when the pass-through is zero (one) the interest rate (the exchange rate) loses its role as an effective instrument.
drive consumers to limit their expenditure in non-tradable goods after a real depreciation (assuming inelastic tradable goods), provoking a negative wealth effect. As in the previous case, if this effect dominates the substitution effect, the depreciation will be contractionary. Moreover, these authors suggest that this dominance is empirically plausible as in emergent economies domestic output has a large services component, which are complementary with respect to tradable goods (both capital and consumption goods), as is shown in the fourth column of Table 4. The wealth effect is reduced under perfect capital mobility as the real balance and external financing restrictions are relaxed.  

The fifth column of Table 4 shows the estimated using a specification close to equation (11). A first observation is that 7 LA economies (out of 14 analyzed) satisfied the definition of financial vulnerability. This illustrates the importance of modeling the wealth effect of depreciations, at least for this group of countries. On the other hand, the ratio of the NPV of debt to investment (second column), a more adequate measure of the debt to investment ratio at the steady state, has a clear relationship with the financial vulnerability measure of these economies as lower ratios correspond to the more robust economies.

Moreover, excluding Chile and Ecuador, the degree of financial vulnerability could be expressed as a function of the ratio of private debt to investment (third column). This is consistent with Céspedes and others (2000). Finally, combining information in Tables 3 and 4, we plot in Figure 3 the relationship between liability dollarization and financial vulnerability. The conclusion is as follows; once emergent economies surpass a threshold (40 percent) the potential contractionary effects of a depreciation are much higher.

![Figure 3. Dollarization and Financial Vulnerability in Latin America](image)

The model dynamics replicates several stylized facts related to monetary policy and external variables in emergent economies. First of all, the effect of the exchange rate on aggregate demand through (6) and (3) has a one-period lag. The expectations effect of this

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33 Caballero (2000) argues that two common factors in fragile emergent economies are the weak links with the international financial system and the limited development of the domestic financial markets. Hausmann and others (2000) pushes forward the idea that the financial vulnerability of these economies is linked to what he call the original sin, i.e. the inability to borrow international in the national currency.
variable has even a longer lag as shown in (1). On the monetary policy side, movements in the interest rate generate short run responses in output in the following period. While from (3), the effect on inflation has a two-period lag. This mechanism is consistent with the short run expansionary effect of monetary policy and with the fact that monetary policy has a long control lag.

Finally, in a financially vulnerable economy, the negative wealth effect of a real exchange rate depreciation is observed one period after the substitution effect. An increase in $q_t$ increases $q_{t+1}$, $y_{t+1}$ and $\varphi_{t+1}$, according to (6), (3) and (11), respectively. The lift in the risk premium increases $l_{t+1}$, $r_{t+1}$ and therefore reduces $y_{t+2}$, following (5), (4), and (3). In the medium term, the positive substitution effect is lower than the negative wealth effect if $\beta_i < \beta$, which is reasonable and plausible.

C. The Central Bank, the Inflation Target, and the Optimal Policy

The Central Bank intervenes in the money market setting a reference interest rate. It’s period preferences are represented by a quadratic loss function \textit{a la} Barro-Gordon, in which all variables are expressed as deviations from their target values\textsuperscript{34},

$$L_t = \pi_t^2 + \chi y_t^2$$

(13)

where $\pi_t$ is the CPI inflation at period $t$. We are assuming that the inflation target measure is a weighted sum between domestic goods and imported goods inflation, which is the common practice among ITers and will probably be the case both in Peru and Uruguay.\textsuperscript{35}

The parameter $\chi$ in equation (13) is a measure of the central bank’s concern about targeting just inflation. Depending on its value we have a central bank that strictly cares about the CPI inflation ($\chi = 0$) or adopt a more flexible position ($\chi > 0$). It can also be included more intermediate regimes if the central bank has other objectives as the smoothness of interest rates or the path of the real exchange rate.\textsuperscript{36}

In order to introduce the CPI inflation into the model framework, we must suppose a share of imported goods inflation, $w$, in the CPI index so

$$\pi_t^c = (1 - w)\pi_t + w\pi_t^f$$

\textsuperscript{34} We will assume that target values coincide with equilibrium levels.

\textsuperscript{35} Calvo (2000) and Mendoza (2000) argue that the inflation targeting is just a fixed exchange rate regime in disguise as the target is a weighted average of domestic prices and the exchange rate.

\textsuperscript{36} Corbo (2000) finds that in the nineties, Chile, Colombia, Costa Rica, El Salvador and Peru, have managed their monetary policies not just looking the inflation rate. He claims that the attention given to other variables (output growth and the real exchange rate) is not just because of improving the predictive power of the inflation rate but those variables represent non formally accepted targets of the monetary policy.
Considering that \( p_t^* = p_t^* + s_t \), the CPI inflation is given by

\[ \pi_t^* = \pi_t + w(q_t - q_{t-1}) \]

Given the target variables, to find the optimal rule, the Central Bank problem is set to minimize,

\[ E_t \sum_{t=0}^{\infty} \delta^t L_t \]  

subject to the dynamics of the economy presented above. As usual, \( \delta \in (0,1) \) is the discount rate and as known, if \( \delta \to 1 \), the limit of (14) is given by the unconditional expectation, that is,

\[ E[L_t] = \text{var}(\pi_t^*) + \lambda \text{var}(y_t) \]  

Since Kydland and Prescott (1977) the discretionary powers of central bank authorities have been under debate. The problem of minimizing (14) is a clear example of that type of behavior and, in a rational expectations framework; we will have a dynamic inconsistency problem. However, the optimality of the discretionary policy is an interesting baseline to evaluate the different strategies that a Central Bank might adopt.

The literature about evaluating alternative monetary policy "fixed" rules has exploded in the last years. However, as we mentioned before there are certain characteristics of the economy that we are considering that warrants the comparison of six different rules, encompassed in the following expression

\[ i_t = f_\pi \pi_t + f_{\pi\pi} \pi_{t+1}/t + f_y y_t + f_q q_{t-1} + f_y y_t \]  

A first group of rules could be dubbed extended Taylor (1993) rules. In all of them set \( f_{\pi1} = 0 \). A first example is the simplest Taylor rule given by (we set \( -f_{q1} = f_q = f_\pi w \)):

\[ i_t = f_\pi \pi_t + f_y y_t \]

A second possibility is to include real exchange movements as a guide in monetary policy decisions \((-f_{q1} = f_q)\), this will render:

\[ i_t = f_\pi \pi_t + f_y y_t + f_q (q_t - q_{t-1}) \]

A third rule is to let all parameters free except for \( f_{\pi1} = 0 \). Therefore the rule could be written as:

\[ i_t = f_\pi \pi_t + f_y y_t + f_{q1} q_{t-1} + f_y y_t \]

A second group of rules are closer cousins of Ball (1999) real interest rate targeting. He emphasizes the importance of considering the exchange rate as an informational variable in a small open economy that is normally buffeted by external shocks, through a

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37 See Battini and others (2000).
Monetary Condition Index. In order to do so, we set \( f_{ni} = 1 \). In this way, our fourth rule could be expressed as:

\[
i_t = \pi_{t+1/t} + f_y \pi_t + f_y y_t + f_q q_{t-1} + f_q q_t
\]

As before, we could restrict this rule to take into account real exchange rate movements and therefore impose the following restrictions \( (f_{x1} = 1, -f_{q1} = f_q) \) to get:

\[
i_t = \pi_{t+1/t} + f_y \pi_t + f_y y_t + f_q (q_t - q_{t-1})
\]

Our last rule is one in which all parameters are free, equation (16).

IV. MODEL PARAMETERIZATION

The model has to be solved numerically as the solution could not be characterized analytically. We calibrate the parameters of the model with estimates from four different countries. In Appendix Table 1 we show the results of those estimations for Australia, New Zealand, Perú, and Uruguay. On the one hand, we used Australia and New Zealand as a benchmark for a financially robust economy. On the other hand, we considered Perú and Uruguay estimates to parameterize the financially vulnerable economy.

The estimated values of the model parameters reflect important differences in the model dynamics of each type of economy. As it is shown in Table 5, robust economies show less inflationary inertia and a higher forward looking component in the inflation rate \( (\alpha_n = 0.3 \text{ in the robust and } 0.5 \text{ in the vulnerable economy}) \). Also, movements in the real exchange rate are more important in vulnerable economies, even though that all four economies used in this study show similar openness ratios and have been subject to the same external shocks (i.e., Asian crisis) in the sample period. In the robust economy, the impact of the exchange rate on the inflation rate in the Phillips curve is 3.5 percent of the inertia coefficient \( (\alpha_n) \) whereas in a vulnerable economy this effect is almost 5 times (17 percent).

In a similar fashion, the impact of the real exchange rate on the output gap, measured in the aggregate demand equation, are quite different. The ratio \( \beta_q / \beta_y \) is 4 percent in the robust case and 7 percent in the vulnerable one. The ratio \( \beta_q / \beta_y \) captures the relative importance of two different channels in the aggregate demand. One is the typical price effect of a real depreciation that increases exports and therefore increases aggregate demand, the other is the impact of monetary policy decisions in the aggregate demand through the typical credit channel. In the robust economy the dominant effect is the latter while in the vulnerable economy the former dominates.

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38 In Latin American central banks the MCI is used only as an indicator and not as an intermediate target.
Table 5. Model Dynamics Relationships of the Robust and Vulnerable Economies

<table>
<thead>
<tr>
<th></th>
<th>Australia</th>
<th>New Zealand</th>
<th>Robust</th>
<th>Peru</th>
<th>Uruguay</th>
<th>Vulnerable</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Aggregate Supply</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$1 - \alpha$</td>
<td>0.73</td>
<td>0.69</td>
<td>0.70</td>
<td>0.55</td>
<td>0.52</td>
<td>0.50</td>
</tr>
<tr>
<td>$\alpha_q / \alpha_q \times 100$</td>
<td>4.9</td>
<td>2.4</td>
<td>3.5</td>
<td>19.0</td>
<td>15.7</td>
<td>17.0</td>
</tr>
<tr>
<td>$\alpha_y / \alpha_y \times 100$</td>
<td>30.3</td>
<td>23.1</td>
<td>25.0</td>
<td>13.1</td>
<td>7.5</td>
<td>10.0</td>
</tr>
<tr>
<td>$\alpha_y \times \beta_y \times 100$</td>
<td>6.6</td>
<td>6.0</td>
<td>6.0</td>
<td>2.4</td>
<td>2.0</td>
<td>2.2</td>
</tr>
<tr>
<td><strong>Aggregate Demand</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\beta_q / \beta_y \times 100$</td>
<td>3.9</td>
<td>4.1</td>
<td>4.0</td>
<td>7.0</td>
<td>6.9</td>
<td>7.0</td>
</tr>
<tr>
<td>$\beta_y / \beta_y \times 100$</td>
<td>11.0</td>
<td>12.2</td>
<td>11.5</td>
<td>87.9</td>
<td>72.8</td>
<td>80.0</td>
</tr>
<tr>
<td>$\beta_q / \beta_y \times 100$</td>
<td>39.1</td>
<td>41.6</td>
<td>40.0</td>
<td>82.3</td>
<td>80.7</td>
<td>80.0</td>
</tr>
<tr>
<td>$\beta_y / \beta_q \times \lambda_{q1}$</td>
<td>-0.02</td>
<td>-0.01</td>
<td>0.0</td>
<td>0.64</td>
<td>1.11</td>
<td>1.08</td>
</tr>
<tr>
<td><strong>Risk Premium Equation</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\lambda_{q1} = \psi_2 - \psi_2$</td>
<td>-0.08</td>
<td>-0.09</td>
<td>-0.09</td>
<td>0.12</td>
<td>0.21</td>
<td>0.17</td>
</tr>
<tr>
<td>$\psi_1 / \beta_q \times 100$</td>
<td>80.5</td>
<td>17.9</td>
<td>50.0</td>
<td>167.2</td>
<td>133.9</td>
<td>150.0</td>
</tr>
<tr>
<td>$\alpha_y / \psi_2 \times 100$</td>
<td>6.4</td>
<td>3.0</td>
<td>4.5</td>
<td>27.7</td>
<td>21.5</td>
<td>25.0</td>
</tr>
</tbody>
</table>

Note: Based on the estimates in Appendix Table 1

In the same vein, the ratio $\beta_q / \beta_y$ measures the importance of the balance sheet channel. The ratio in the robust economy is 0 percent, whereas in the vulnerable economy the impact of the real exchange rate relative to the impact of the interest rate on aggregate demand is 1.08 percent. Finally, while in a robust economy the impact of external demand shock represents 11.5 percent of the domestic shocks ($\beta_q / \beta_y$) in the vulnerable economy this figure is 80 percent.

The ratio $\psi_1 / \beta_q$ could be thought as the basis points decreased (increased) in the risk premium vis-à-vis an increase (decrease) in output given a positive (negative) shock in the external demand. In a robust economy this ratio is 50 percent while in a vulnerable economy is 150 percent. Finally, the ratio $\alpha_q / \psi_2$ reflect the increase in inflation vs. the increase in the risk premium in the event of a real depreciation. While for the robust economy the ratio is 4.5 percent, a vulnerable economy has a ratio of 25 percent.

Based on these ratios and relationships the parameter values used for the simulations are reported in Table 6. It is important to emphasize that the differences between a robust and a vulnerable economy lie on the differences in the risk premium equation and in the importance of domestic vis-à-vis external shocks. In order to compare the simulated variances, we set all shock variances to 0.5, excepting the Phillips curve and aggregate demand that are set to 1.0. Finally, the share of imported goods in the CPI inflation is set to $\omega = 0.3$. 
Table 6. Baseline Parameters for Robust and Vulnerable Economies

| Aggregate Supply and Aggregate Demand  
<table>
<thead>
<tr>
<th>(1), (5) and (3)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Robust</td>
</tr>
<tr>
<td>( \alpha_x )</td>
</tr>
<tr>
<td>( \alpha_y )</td>
</tr>
<tr>
<td>( \alpha_q )</td>
</tr>
<tr>
<td>( \beta_y )</td>
</tr>
</tbody>
</table>

Risk Premium Equation and External Variables  
(16), (11), (12) and (13)

<table>
<thead>
<tr>
<th>Robust</th>
<th>Vulnerable</th>
<th>Both</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \psi_1 )</td>
<td>0.046</td>
<td>0.528</td>
</tr>
<tr>
<td>( \psi_2 )</td>
<td>0.233</td>
<td>0.340</td>
</tr>
<tr>
<td>( \psi_3 )</td>
<td>0.148</td>
<td>0.509</td>
</tr>
<tr>
<td>( \lambda_{\epsilon q} )</td>
<td>-0.086</td>
<td>0.169</td>
</tr>
</tbody>
</table>

V. MODEL SOLUTION AND SIMULATIONS

In this section we present three exercises in order to answer the question of which is the best way to conduct an IT regime conditional on the economy type. First of all, we compute the optimal policy rule without restrictions on the set of policy indicators. Then, we restrict our attention to fixed rules in which a much narrow set of indicators is used to guide monetary policy. Instead of calibrate the parameters associated with those rules we compute optimized coefficients for each rule. Finally, we study the optimality of a non linear policy rule for the financially vulnerable economy case.

A. The Optimal Rule

Given a baseline assumption that \( \chi = 0.5 \), the optimal policy rule for each case is shown in Table 7. As the central bank cares about the CPI inflation, the reaction function includes almost all variables in the system as the real exchange rate is a forward looking variable.\(^{39}\)

The coefficient on expected inflation is larger in the robust economy as we expect because of less inflationary inertia in the robust economy vis-à-vis the vulnerable economy. One of the most important variables in the vulnerable economy is the risk premium. This is completely as expected as fluctuations in the risk premium transmit that volatility to the output gap, the real exchange rate and inflation. In general, the vulnerable economy shows

\(^{39}\) This represents a trade-off for the central bank as it is much more transparent to target the CPI inflation but is much easier to comply with a domestic inflation target. In a heavily dollarized economy is obvious that market participants will question the response of the central bank regarding the exchange rate.
higher coefficients in all external variables. One striking result is the fact that the output gap plays almost no role in the reaction function in the vulnerable economy case.

### Table 7. Optimal Rule for Robust and Vulnerable Economies

<table>
<thead>
<tr>
<th>Economy</th>
<th>$\pi_t$</th>
<th>$y_t$</th>
<th>$\pi^*_t$</th>
<th>$y^*_t$</th>
<th>$i^*_t$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Robust</td>
<td>1.508</td>
<td>0.643</td>
<td>-0.447</td>
<td>0.086</td>
<td>0.440</td>
</tr>
<tr>
<td>Vulnerable</td>
<td>1.369</td>
<td>0.067</td>
<td>-0.587</td>
<td>0.432</td>
<td>0.524</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Economy</th>
<th>$\varphi_t$</th>
<th>$q_{t-1}$</th>
<th>$\pi_{t+1/t}$</th>
<th>$q_{t/t-1}$</th>
<th>$y_{t/t-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Robust</td>
<td>0.590</td>
<td>-0.422</td>
<td>0.244</td>
<td>-0.065</td>
<td>0.022</td>
</tr>
<tr>
<td>Vulnerable</td>
<td>1.197</td>
<td>-0.411</td>
<td>0.071</td>
<td>-0.291</td>
<td>0.343</td>
</tr>
</tbody>
</table>

The variances of the most relevant variables under an optimal rule are:

### Table 8. Unconditional Standard Deviations Under the Optimal Rule

<table>
<thead>
<tr>
<th>Economy</th>
<th>$\pi^*_t$</th>
<th>$\pi_t$</th>
<th>$y_t$</th>
<th>$i_t$</th>
<th>$r_t$</th>
<th>$q_t$</th>
<th>$E[L_t]$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Robust</td>
<td>1.868</td>
<td>1.440</td>
<td>1.930</td>
<td>2.331</td>
<td>3.971</td>
<td>3.768</td>
<td>3.936</td>
</tr>
<tr>
<td>Vulnerable</td>
<td>3.265</td>
<td>2.044</td>
<td>2.189</td>
<td>3.216</td>
<td>5.410</td>
<td>8.888</td>
<td>6.574</td>
</tr>
</tbody>
</table>

As expected the robust economy is significantly less volatile than the vulnerable one. There is more structural volatility in the robust economy. In particular, the major source of volatility in the vulnerable economy comes from real exchange rate fluctuations. We simulate in Figure 4 the variance frontiers for both economies with different preferences in the loss function. A low value of $\chi$ represents a "hawkish" central, while a value of $\chi = 1$ represents a "dove" central bank that is more concerned about the output gap instead of the inflation rate. A first result is the variance dominance of the robust economy compared to a financially vulnerable economy.

Figure 4. Variance Frontiers for Robust and Vulnerable Economies Under the Optimal Rule
As shown in Figure 4 a central bank too hawkish may exacerbate the volatilities of the real exchange rate and the real interest rate. The reason behind might be that the central bank has to behave in a much more discretionary form if chooses to be too hawkish. In particular, it will be willing to intervene in the money market and in the exchange rate market to stop any deviation in the inflation target. This evidence suggests that it might be optimal to have a flexible IT regime (as the baseline assumption) instead of a strict one.

B. Alternative Rules

As our goal is try to shed some light in which type of rules might be optimal for economies in which balance sheet effects matter we simulate the six types of rules presented in the above section for both classes of economy. The results (optimized coefficients) are presented in Table 9 and in Table 10 we present the variances associated with those optimized rules.

We can draw several conclusions out of this simulation exercise. First of all, in both economies Ball-type rules are superior. However, this is much clearer in the vulnerable economy where the difference of including the real exchange rate depreciation is significant. Another expected and clear result is that simpler rules come with a price in terms of higher volatility. Again the difference is much stronger in the vulnerable economy. This might support the hypothesis that in vulnerable economies make sense to look a wider set of indicators to design the monetary policy, with special attention in the exchange rate.

<table>
<thead>
<tr>
<th>Rule</th>
<th>( f_{s1} = 0, -f_{s1} = f_q = f_{s1} )</th>
<th>( \pi_t )</th>
<th>( \pi_{t+1/t} )</th>
<th>( y_t )</th>
<th>( q_{t-1} )</th>
<th>( q_t )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rule 1</td>
<td>1.217</td>
<td></td>
<td>0.208</td>
<td>-0.365</td>
<td>0.365</td>
<td></td>
</tr>
<tr>
<td>Rule 2</td>
<td>1.152</td>
<td></td>
<td>0.259</td>
<td>-0.228</td>
<td>0.228</td>
<td></td>
</tr>
<tr>
<td>Rule 3</td>
<td>0.836</td>
<td></td>
<td>0.380</td>
<td>-0.202</td>
<td>0.549</td>
<td></td>
</tr>
<tr>
<td>Rule 4</td>
<td>1.878</td>
<td>1.000</td>
<td>0.830</td>
<td>-0.536</td>
<td>0.536</td>
<td></td>
</tr>
<tr>
<td>Rule 5</td>
<td>1.106</td>
<td>1.000</td>
<td>0.396</td>
<td>-0.236</td>
<td>0.507</td>
<td></td>
</tr>
<tr>
<td>Rule 6</td>
<td>Unrestricted parameters</td>
<td>0.741</td>
<td>0.783</td>
<td>-0.338</td>
<td>0.403</td>
<td></td>
</tr>
</tbody>
</table>

Table 9. Simple Fixed Rules for Robust and Vulnerable Economies
Table 10. Unconditional Standard Deviations Under Alternative Fixed Rules

<table>
<thead>
<tr>
<th>Robust Economy</th>
<th>$\pi_t$</th>
<th>$\pi_t^c$</th>
<th>$y_t$</th>
<th>$i_t$</th>
<th>$r_t$</th>
<th>$q_t$</th>
<th>$E[L_t]$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rule 1</td>
<td>1.874</td>
<td>1.989</td>
<td>2.177</td>
<td>5.331</td>
<td>6.081</td>
<td>4.876</td>
<td>4.362</td>
</tr>
<tr>
<td>Rule 2</td>
<td>1.826</td>
<td>1.938</td>
<td>2.173</td>
<td>5.403</td>
<td>5.956</td>
<td>5.060</td>
<td>4.308</td>
</tr>
<tr>
<td>Rule 3</td>
<td>1.109</td>
<td>1.486</td>
<td>2.190</td>
<td>5.750</td>
<td>6.287</td>
<td>2.619</td>
<td>3.467</td>
</tr>
<tr>
<td>Rule 4</td>
<td>1.517</td>
<td>1.468</td>
<td>2.183</td>
<td>6.048</td>
<td>6.564</td>
<td>0.771</td>
<td>4.172</td>
</tr>
<tr>
<td>Rule 5</td>
<td>1.113</td>
<td>1.487</td>
<td>2.190</td>
<td>5.738</td>
<td>6.275</td>
<td>2.638</td>
<td>3.464</td>
</tr>
<tr>
<td>Rule 6</td>
<td>1.122</td>
<td>1.482</td>
<td>2.189</td>
<td>5.712</td>
<td>6.245</td>
<td>2.653</td>
<td>3.459</td>
</tr>
<tr>
<td>Optimal</td>
<td>1.951</td>
<td>1.742</td>
<td>1.808</td>
<td>3.215</td>
<td>4.448</td>
<td>3.003</td>
<td>3.237</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Vulnerable Economy</th>
<th>$\pi_t^c$</th>
<th>$\pi_t$</th>
<th>$y_t$</th>
<th>$i_t$</th>
<th>$r_t$</th>
<th>$q_t$</th>
<th>$E[L_t]$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rule 2</td>
<td>2.644</td>
<td>2.066</td>
<td>2.810</td>
<td>3.645</td>
<td>4.166</td>
<td>4.778</td>
<td>6.134</td>
</tr>
<tr>
<td>Rule 3</td>
<td>2.128</td>
<td>2.340</td>
<td>2.822</td>
<td>3.180</td>
<td>3.727</td>
<td>2.128</td>
<td>4.761</td>
</tr>
<tr>
<td>Rule 4</td>
<td>2.078</td>
<td>2.711</td>
<td>2.785</td>
<td>3.163</td>
<td>3.848</td>
<td>3.658</td>
<td>4.598</td>
</tr>
<tr>
<td>Rule 5</td>
<td>2.113</td>
<td>2.340</td>
<td>2.895</td>
<td>3.200</td>
<td>3.735</td>
<td>2.168</td>
<td>4.840</td>
</tr>
<tr>
<td>Rule 6</td>
<td>2.086</td>
<td>2.340</td>
<td>2.484</td>
<td>3.171</td>
<td>3.723</td>
<td>2.097</td>
<td>4.221</td>
</tr>
<tr>
<td>Optimal</td>
<td>2.177</td>
<td>2.315</td>
<td>2.211</td>
<td>3.018</td>
<td>3.331</td>
<td>4.192</td>
<td>4.047</td>
</tr>
</tbody>
</table>

C. On the Optimality of a (Nonlinear) Fear of Floating Rule

Lahiri and Végh (2001) show that in economies in which fluctuations in the real exchange rate might cause serious damage in terms of output it will be optimal to follow a fear on floating rule. This is a non-linear policy rule that calls for a different response conditional on the size of the shock. If the shock is severe the optimal policy is to avoid completely any perturbation of the real exchange rate whereas if the shock is small the rule will suggest "let the currency float".

We try a similar non-linear rule for the vulnerable economy to study if we can find supporting evidence to the theoretical model of Lahiri and Végh (2001). Based on rule 4, we simulate the following non-linear monetary policy rule:

$$i_t = f_\pi \pi_t + f_\pi \pi_{t+1}/t + f_y y_t + f_q (q_{t+1}/t - q_t) \quad \text{if} \quad q_{t+1}/t - q_t \leq \bar{q}$$

$$i_t = f_\pi \pi_t + f_\pi \pi_{t+1}/t + f_y y_t + (f_q + \theta_q)(q_{t+1}/t - q_t) \quad \text{if} \quad q_{t+1}/t - q_t > \bar{q}$$

The idea is that the monetary authority will follow the linear rule only if the real exchange rate depreciation does not exceed to a certain threshold ($\bar{q}$). If the shock is larger than the threshold, the authorities will set a stricter monetary policy stance. The intensity of this response is defined by $\theta_q$. The logic is simple and reminiscent of what central bankers in the region do in turbulent times.

We compare this non-linear policy with the optimal linear policy that we found in our previous analysis. To capture in a simple way we construct a variance ratio:
\[ v = \frac{\text{var}(x^{\text{Nonlinear}})}{\text{var}(x^{\text{optimal}})} \]

where \( x \) is a particular variable of interest. Therefore when the variance ratio \( v < 1 \) the *non-linear rule* would be better compared to the optimal linear rule. We want to obtain a relationship between the key parameters of the non-linear policy rule \((\theta_g, \bar{q})\) and the optimal policy rule.

With this in mind we simulate \( T = 1000 \) periods of the model. We generate data that comes out of the model assuming normal errors with unit variance and nondiagonal var-cov matrix. We did 10,000 repetitions of this experiment and report the mean values. We performed the simulations for three different values of the threshold value (0.01, 1.50, and 3.00) and plot in Figure 5 the variance ratios for different values of the response intensity parameter.

In each panel, we explore the optimality of the non-linear vis-à-vis the best linear policy. As we can see the non-linear rule is optimal for a significant part of the parameter space. A larger concern for the real exchange rate generates more volatility in domestic inflation, but less volatility on the CPI inflation. This result depends on the pass-through intensity. But it also depends on the adverse effect of the balance sheet channel. As the real exchange rate volatility is lower, the risk premium volatility goes down whereas the output gap volatility is almost the same in both policy rules.

Interestingly, as the threshold value is smaller, the volatilities of all variables are lower. The \( \bar{q} = 0.01 \) case should be thought as an almost fixed exchange regime. This result should come with a warning. We are not considering in the model the pervasive dynamics that comes out of following a *fear of floating* rule. If the central bank consistently avoids large fluctuations in the exchange rate will incentive firms and households to have a larger exposure to dollar denominated liabilities. Thus, the economy will become even more vulnerable as before. Obviously, this is one issue that we need to explore is the optimality of this policy with a model that takes into account this effect. And for that matter we are also ignoring the possible costs in terms of losing reserves responding to the external shocks.

If we rule out the almost fixed exchange rate case, we will find supporting evidence to the claim that in the case of a financially vulnerable economy it makes sense to have a non-linear monetary policy rule that defends the exchange rate with a stronger response in the case of turbulent times but allows the exchange rate to float in tranquil times. In the last panel we show the behavior of the variance ratio for the loss function of the central bank. In that panel we can see that the optimal response intensity is to add an extra 60 basis points to the interest rate given a one percent depreciation in the real exchange rate.
This paper has been written from the perspective of the central bank that chooses to adopt an IT regime within a very special set of initial conditions: an emergent economy with highly dollarized liabilities. Therefore, we have addressed the issue assuming that the Central Bank has chosen to “walk the talk” and we explore the optimal way to do that within a simple small, open-economy model that captures the striking characteristics of the economy. For that purpose, we compare the optimality of several alternative rules.

We calibrate the model for two types of economy after considering explicitly the possibility of a financially robust and a financially vulnerable economy, as suggested by Cespedes and others (2000) and Gertler and others (2001). In the latter case, real exchange rate fluctuations may have pervasive real effects. We use data for Australia and New Zealand to calibrate the robust economy and Peruvian and Uruguayan data for the financially vulnerable case. We found empirical support for the hypothesis of a financially vulnerable economy, as suggested by Cespedes and others (2000), as the risk premium-real exchange rate elasticity is -0.10 in the robust case and 0.15 in the vulnerable case.

Along that same line, our main result suggests the optimality of defending the real exchange rate if the economy is financially vulnerable. However, the real exchange rate cannot be a target of monetary policy in the long run. There is no way that monetary policy could influence a real variable in the long run. Even though in the short term there might be some effectiveness in appreciation or depreciation of the exchange rate, in the long run this will be reversed.
The perils of following unsustainable policies are that they promote (instead of curb) behavior that will add (in the future) more vulnerability to the economy. For example, if the central bank bails out the banks or firms consistently to avoid financial distress, they will take on much greater risk, worsening the balance-sheet issues. The same thing happens if the central bank has an implicit defense of the exchange rate within a flexible inflation-targeting framework, like the nonlinear rule presented in section 5.3. Instead of fostering more hedging, they will end up having more open positions in foreign currency. If the inflation targeting turns out to be exchange rate targeting in disguise, the balance-sheet effects will tend to be stronger, since this will provide an incentive to underinsure against depreciation risk or take on more dollar-denominated debt. The inflation targeting might work in terms of attaining the targets, but the consequences might be that firms become more prone to increase their dollar-denominated debts as governments show they are reluctant to let them go bankrupt. This calls for further research on the feasibility of using IT regimes in highly dollarized economies. Specifically, this research should determine the factors behind the threshold up to which the central banks are willing to follow a fully flexible exchange rate regime.

Even though one possible gain from adopting an IT strategy is that it extends the relevant horizon of the monetary policy, it is still a very imperfect mechanism with which to tackle unresolved issues in financially vulnerable economies. It might be quite useful to guide inflation expectations but, a priori, not to solve liability dollarization issues. This might go against the intuition that in the context of low and stable inflation (the typical initial conditions of countries that have adopted IT), the growth of domestic money demand will reduce the dollarization ratio. However, this effect has not been systematically observed in the data. Moreover, the vulnerable economies analyzed here have shown significant reductions in the inflation rate and its volatility without much changes in the initial dollarization ratios. Of course, only time will tell how well IT frameworks fare in dollarized economies.
A. Data

We use monthly data from the IMF from January 1990 to June 2001, except in the case of Perú in which the database starts in January 1992, because of the high inflation rates at the beginning of the 90s. The variables included are, following IMF definitions, the nominal exchange rate, the discount rate in domestic currency, the CPI inflation, the real GDP (1995 = 100), the CPI of the USA, the USA index of industrial output, and the 3-month LIBOR rate. In all cases the GDP data is published quarterly, except in Perú in which the GDP index is published monthly by the Central Bank. In order to use monthly data we used the Chow and Lin extrapolation technique, as explained in Robertson and Tallman (1999). With these data, the model variables were computed in the following way:

\[ s = \log \text{nominal exchange rate minus its HP trend.} \]
\[ \pi = \text{year-to-year variation of CPI (demeaned)} \]
\[ \pi^* = \text{year-to-year variation of USA CPI (demeaned)} \]
\[ y = \text{demeaned annual growth rate of real GDP.} \]
\[ y^* = \text{Demeaned US Industrial Production Index rate of annual growth.} \]
\[ q = \text{Computed following (4)} \]

The expected variables were instrumented as in Clarida and others (1998, 2000) and are the recursive h-step-ahead forecasts from a multivariate VAR with all the variables listed before. Once we determine \( s_{t+1/t} \) we calculate the risk premium according to (5).

B. The State-Space Form of the Model

To solve the model we must express it in its state-space form. It can be shown that the model has the following representation (see Svensson (2000) and Leitemo (1999) for a detailed exposition):

\[
\begin{bmatrix}
X_{t+1} \\
X_{t+1/t}
\end{bmatrix} = A \begin{bmatrix} X_t \\ x_t \end{bmatrix} + B_0 i_t + B_1 i_{t+1/t} + \begin{bmatrix} v_{t+1} \\ 0 \end{bmatrix} \tag{A.1}
\]
\[ Y_t = C_1 \begin{bmatrix} X_t \\ x_t \end{bmatrix} + C_2 i_t \tag{A.2} \]
\[ L_t = Y_t' KY_t' \tag{A.3} \]

where \( X_t \) denotes a column vector of predetermined state variables, \( x_t \) is a vector of forward-looking variables, \( Y_t \) is the vector of target variables and \( v_t \) is the vector of innovations of \( X_t \),

\[ X_t = (\pi_t, y_t, \pi^*_t, y^*_t, i_t, \rho_t, y''_t, q_{t-1}, q_{t-1/t}, \pi_{t-1/t}, q_{t-1/t-2}, \pi_{t-1/t-1}, e_{t-1}, y_{t-1/t-1})' \]
\[ x_t = (\pi^*_t, y_t)’ \]
\[ Y_t = (\pi^*_t, y_t)’ \]
\[ v_t = (\epsilon_t, \eta_t^d - \eta_t'' - \epsilon_t^d, \eta_t^*, f^*_\pi \epsilon_t + f^*_\pi^* \epsilon_t^* + \xi^*_t, \xi^*_t, \eta_t^*, 0, 0, \alpha_x \epsilon_t + \alpha_y \eta_t (\eta_t^d - \eta_t''), 0, 0, 0, 0, 0)' \]
B. The State-Space Form of the Model

To solve the model we must express it in its state-space form. It can be shown that the model has the following representation (see Svensson (2000) and Leitemo (1999) for a detailed exposition):

\[
\begin{bmatrix}
X_{t+1} \\
x_{t+1} \\
\end{bmatrix} = \begin{bmatrix}
A & B \\
0 & I \\
\end{bmatrix} \begin{bmatrix}
X_t \\
x_t \\
\end{bmatrix} + \begin{bmatrix}
B_0 i_t + B_1 i_{t+1} \\
0 \\
\end{bmatrix} + \begin{bmatrix}
v_t \\
v_{t+1} \\
\end{bmatrix}
\]

(A.1)

\[Y_t = C_1 \begin{bmatrix}
X_t \\
x_t \\
\end{bmatrix} + C_2 i_t
\]

(A.2)

\[L_t = Y_t^\prime K Y_t
\]

(A.3)

where \(X_t\) denotes a column vector of predetermined state variables, \(x_t\) is a vector of forward-looking variables, \(Y_t\) is the vector of target variables and \(v_t\) is the vector of innovations of \(X_t\),

\[
X_t = (\pi_t, y_t, \pi_t^*, i_t^*, i_t, \phi_t, y_t^*, q_{t-1}, i_{t-1}, \pi_{t+1/4}, q_{t-1/4}, i_{t-1/4}, \pi_{t-1/4}, \epsilon_{t-1}, y_{t-1})'
\]

\[
x_t = (q_t, \rho_t, \pi_{t+2/4})'
\]

\[
Y_t = (\pi_t, y_t)'
\]

\[
v_t = (\epsilon_t, \eta_t, \pi_t, \eta_t^*, \pi_t^*, \phi_t, y_t^*, q_{t-1}, i_{t-1}, \pi_{t+1/4}, q_{t-1/4}, i_{t-1/4}, \pi_{t-1/4}, \epsilon_{t-1}, y_{t-1})'
\]

Additionally if \(n_1 = \text{dim}(X_t), n_2 = \text{dim}(x_t), n_3 = \text{dim}(Y_t)\) and \(n = n_1 + n_2\), \(A\) is a coefficient \(n\) matrix, \(B_0\) and \(B_1\) are \(n \times 1\) vectors of coefficients, \(C_1\) is a \(n_3 \times n\) matrix, \(C_2\) is a \(n_3 \times 1\) vector and \(K\) is a \(n_3\) diagonal matrix which elements correspond to the weights of equation (13).

Given the linearity of the model (A.1) – (A.3), the dynamics of this economy could be expressed exclusively in terms of the predetermined variables,

\[
X_{t+1} = G_{11} X_t + v_{t+1}
\]

(A.4)

\[x_t = HX_t
\]

(A.5)

\[i_t = fX_t
\]

(A.6)

\[Y_t = (C_{11} + C_{12} H + C_2 f) X_t
\]

(A.7)

where, following Svensson (2000), the \(n\) matrix \(G\) is defined as:

\[
G = (I - B_1 F)^{-1}
\begin{bmatrix}
A & 0 \\
H & 0 \\
\end{bmatrix} + B_0 F
\]

with \(F = (f, 0, 0, 0)\) and the matrices \(G\) and \(C_1\) are partitioned according to \(X_t\) and \(x_t\).

The representation (A.4) – (A.7) helps us to understand the logic of the model. From a discretionary perspective, \(f\) and \(H\) are endogenously determined so as to minimize (19) (like a standard linear-quadratic regulator problem, that implies iterations over a Ricatti equation). Contrarily, if the central bank has committed to follow a fixed rule, the vector \(f\) is determined exogenously and the system is solved just for \(H\), using the solution algorithms proposed by Sims (1998) and Klein (2000).
Appendix Table 1. SUR Estimates for Robust and Vulnerable Economies

<table>
<thead>
<tr>
<th></th>
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<tbody>
<tr>
<td><strong>Aggregate Supply</strong></td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha_x$</td>
<td>0.2853 (2.0356)</td>
<td>0.3056 (18.0269)</td>
<td>0.4504 (15.5102)</td>
<td>0.4614 (46.8197)</td>
</tr>
<tr>
<td>$\alpha_y$</td>
<td>0.0604 (3.1182)</td>
<td>0.0706 (8.6473)</td>
<td>0.0588 (3.6614)</td>
<td>0.0663 (8.6053)</td>
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<tr>
<td>$\alpha_z$</td>
<td>0.0131 (2.3237)</td>
<td>0.0007 (0.7814)</td>
<td>0.0054 (2.0162)</td>
<td>0.0754 (2.8269)</td>
</tr>
<tr>
<td>Standard Error of $\epsilon$</td>
<td></td>
<td></td>
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<tr>
<td>Residuals Jarque-Bera stat</td>
<td>0.2994</td>
<td>0.2852</td>
<td>0.8990</td>
<td>0.7026</td>
</tr>
<tr>
<td>Adjusted R-squared</td>
<td>0.0925</td>
<td>0.6114</td>
<td>4.2928</td>
<td>6.0723</td>
</tr>
<tr>
<td>Durbin-Watson stat</td>
<td>1.7197</td>
<td>1.0934</td>
<td>1.7547</td>
<td>2.0915</td>
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<td><strong>Aggregate Demand and Output Gap</strong></td>
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<tr>
<td>$\beta_y$</td>
<td>0.8262 (15.6735)</td>
<td>0.8246 (28.4136)</td>
<td>0.4025 (2.6523)</td>
<td>0.5367 (9.4528)</td>
</tr>
<tr>
<td>$\beta_r$</td>
<td>0.0613 (1.0118)</td>
<td>0.0842 (1.3526)</td>
<td>0.0344 (1.7842)</td>
<td>0.0462 (2.7948)</td>
</tr>
<tr>
<td>$\beta_y^*$</td>
<td>0.0970 (0.9314)</td>
<td>0.1041 (2.4235)</td>
<td>0.3545 (8.8528)</td>
<td>0.3923 (1.6960)</td>
</tr>
<tr>
<td>$\beta_r^*$</td>
<td>0.0318 (2.0715)</td>
<td>0.0350 (2.7090)</td>
<td>0.0283 (1.1290)</td>
<td>0.0372 (2.6847)</td>
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<tr>
<td>$\beta_x^*$</td>
<td>0.0073 (0.4585)</td>
<td>0.0052 (0.2816)</td>
<td>0.1450 (1.5103)</td>
<td>0.1943 (1.4386)</td>
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<tr>
<td>Standard Error of $\gamma$</td>
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<tr>
<td>Residuals Jarque-Bera stat</td>
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<td>5.1972</td>
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<td>Durbin-Watson stat</td>
<td>1.0203</td>
<td>2.1975</td>
<td>2.2398</td>
<td>1.8013</td>
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<td><strong>Risk Premium Equation</strong></td>
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<tr>
<td>$\psi_1$</td>
<td>0.0720 (9.8035)</td>
<td>0.0186 (0.1336)</td>
<td>0.5917 (2.1503)</td>
<td>0.5252 (1.4682)</td>
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<tr>
<td>$\psi_2$</td>
<td>0.2040 (5.7531)</td>
<td>0.2503 (8.8529)</td>
<td>0.3060 (1.6531)</td>
<td>0.0514 (2.2765)</td>
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<tr>
<td>$\psi_3$</td>
<td>0.1210 (1.8414)</td>
<td>0.1622 (2.2117)</td>
<td>0.4324 (1.1148)</td>
<td>0.3610 (2.3293)</td>
</tr>
<tr>
<td>Standard Error of $\xi$</td>
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<td></td>
</tr>
<tr>
<td>Residuals Jarque-Bera stat</td>
<td>1.0948</td>
<td>1.0712</td>
<td>1.0740</td>
<td>1.6623</td>
</tr>
<tr>
<td>Adjusted R-squared</td>
<td>0.0272</td>
<td>5.2764</td>
<td>1.0248</td>
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<tr>
<td>Durbin-Watson stat</td>
<td>2.4573</td>
<td>2.3269</td>
<td>2.1899</td>
<td>2.4804</td>
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<tr>
<td><strong>External Variables</strong></td>
<td>Standard Deviations of Residuals</td>
<td>Residuals Jarque-Bera</td>
<td>Adjusted R-squared</td>
<td>Durbin-Watson stat</td>
</tr>
<tr>
<td>Inflation</td>
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<tr>
<td>$\gamma^*_x$</td>
<td>0.9540 (7.2855)</td>
<td>0.1559</td>
<td>1.8150</td>
<td>0.9112</td>
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<tr>
<td>Demand</td>
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<tr>
<td>$\gamma^*_y$</td>
<td>0.8699 (5.0452)</td>
<td>0.6098</td>
<td>3.1658</td>
<td>0.7887</td>
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<td>Interest Rate</td>
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<tr>
<td>$f^*_x$</td>
<td>0.7604 (5.0344)</td>
<td>0.4853</td>
<td>2.2987</td>
<td>0.2982</td>
</tr>
<tr>
<td>$f^*_y$</td>
<td>0.4254 (6.6773)</td>
<td>0.4853</td>
<td>2.2987</td>
<td>0.2982</td>
</tr>
</tbody>
</table>

- 30 –
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