Drivers of Peru's Equilibrium Real Exchange Rate: Is the Nuevo Sol a Commodity Currency?

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Melesse Tashu

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Western Hemisphere Department

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Prepared by Melesse Tashu*

Authorized for distribution by Alejandro Santos

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Abstract

This paper tests the hypothesis of ‘commodity currency’ on the nuevo sol and, more generally, identifies the drivers of Peru’s equilibrium real exchange rate using a cointegration analysis. The results show that export commodity prices do not have a statistically significant impact on Peru’s real effective exchange rate, suggesting that the nuevo sol is not a commodity currency. The paper provides empirical evidence that large profit repatriation and foreign exchange intervention have effectively insulated Peru’s real exchange rate from the impact of commodity price shocks. Peru’s equilibrium real exchange rate is found to be driven mostly by productivity and government consumption.

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Author’s E-Mail Address: mtashu@imf.org

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I. INTRODUCTION

Since the real exchange rate¹ is the relative price of tradable and non-tradable goods in an economy, understanding whether it is in line with the equilibrium level is important for efficient allocation of resources between the tradable and non-tradable sectors. A misaligned real exchange rate, i.e. a real exchange rate that deviates substantially from the equilibrium level, could create large macroeconomic imbalances and distort incentives and allocation of resources by sending wrong signals to economic agents.

While the equilibrium real exchange rate is an unobservable variable, economic theory suggests that it is driven by such observable economic fundamentals as the terms of trade (or the real prices of key export commodities for commodity dependent economies), relative productivity of tradables to non-tradables, government consumption, and the net foreign asset position. For commodity dependent economies like Peru, in particular, the equilibrium real exchange rate is conjectured to be primarily determined by the real prices of export commodities so much that their currencies are commonly referred to as ‘commodity currencies’ (Chen and Rogoff, 2003; Cashin et al, 2004; Bodart et al, 2012).

The essential step in estimating the equilibrium real exchange rate is establishing an econometric relationship between the real exchange rate and the fundamentals, which is the main objective of this study. In particular, the study aims to test if Peru’s real exchange rate is primarily determined by the real prices of key export commodities as the ‘commodity currency’ hypothesis would suggest. To achieve this objective, the study employs the Johansen cointegration method. Robustness of the results is tested with various specifications, including with alternative definitions of the real exchange rate and real commodity prices, varying sample sizes, and alternative methodologies.

The paper also attempts to estimate the path of the notional equilibrium real exchange rate using the estimated long-run cointegration relationship between the real exchange rate and the fundamentals. The equilibrium real exchange rate estimated in this study, however, does not have a normative implication as it does not necessarily imply optimality from a welfare perspective. A normative assessment of the equilibrium real exchange rate requires making judgments on the optimality of the values of the fundamentals, which is beyond the scope of this study.

The study is organized as follows. The theoretical framework is presented in Section II, followed by the empirical model and data description in Section III. Section IV presents the estimation results and Section V concludes the study.

¹ The terminologies ‘real exchange rate’ and ‘real effective exchange rate’ both of which refer to the exchange rate of the nuevo sol against a basket of currencies of major trading partner countries adjusted for price differentials between Peru and trading partner countries are used interchangeable in this study.

II. THEORETICAL FRAMEWORK

Attempts to model the equilibrium real exchange rate goes back to the Purchasing Power Parity (PPP) theory, which states in its absolute form that the exchange rate between currencies of two countries is simply given by the relative price levels expressed in the same currency (i.e., generalization of the law of one price); and in its relative form, the theory asserts that the percentage change in the exchange rate between two currencies is determined by the inflation differential between the corresponding countries. In its weakest form, the PPP hypothesis requires deviations from the PPP real exchange rate to die out eventually and the real exchange rate to be stable, exhibiting a stationery or mean reverting property in the long run (Rogoff, 1996; Astorga, 2012). If this was true, the equilibrium real exchange rate would be constant and could be represented by the long-run or PPP real exchange rate. However, the PPP hypothesis received very little empirical support, especially in the short run, as most studies show that real exchange rate deviations are persistent and the real exchange rate exhibits a unit root process (Meese and Rogoff, 1983; Rogoff, 1996; Engel, 2000; Astorga, 2012).

The empirical failure of the PPP theory, referred in the literature as the PPP puzzle, has led to the hypothesis that the equilibrium real exchange rate could be time varying driven by real factors or fundamentals. In a seminal paper on the PPP puzzle, Rogoff (1996) argues that the high short-term volatility of the real exchange rate and the very slow adjustment of shocks to PPP are so irreconcilable that the deviations from PPP must be accounted for by real factors. Such real factors that are hypothesized to drive the equilibrium real exchange rate include the terms of trade (or real prices of commodities for commodity dependent economies), the relative productivity of tradables to non-tradables, government consumption, and net foreign asset position (Froot and Rogoff, 1995; Rogoff, 1996; Montiel, 2007; Ricci et al, 2013).

- (i) *Real price of commodities*: While the terms of trade is generally used in real exchange rate models, for commodity dependent small open economies the real price index of key export commodities is a more relevant variable. As Chen and Rogoff (2003) indicate aggregate export and import price indices used to construct the terms of trade include goods with sluggish nominal price adjustments and incomplete pass-through, leading to identification problems in econometric estimations. On the contrary, world commodity prices are purely exogenous for small exporting economies as they are determined at the world markets. An increase in commodity prices can lead to wage increases in the commodity sector, and across the economy since labor is assumed to be mobile, leading to an increase in the relative price of non-tradables as the price of tradables is determined in the world market and, therefore, to a real exchange rate appreciation (Chen and Rogoff, 2003; Cashin et al, 2004).
- (ii) *Relative productivity of tradables to non-tradables*: According to the Balassa-Samuelson hypothesis (Balassa, 1964; Samuelson, 1964), an increase in the relative productivity of tradables to non-tradables will drive up economy-wide wages,

- (iii) assuming labor is mobile between the two sectors, resulting in a higher relative price of non-tradables (i.e., a real appreciation).
- (iv) *Net foreign asset position*: an increase in net foreign liabilities will require a more depreciated real exchange rate to generate the trade surplus necessary to service the external debt (Rogoff, 1996; Ricci et al, 2013).
- (v) *Government consumption*: higher government consumption is likely to lead to an appreciation of the equilibrium real exchange rate since government consumption tends to fall more on nontradables than tradables (Froot and Rogoff, 1995; Rogoff, 1996; Ricci et al, 2013).

III. EMPIRICAL MODEL AND DATA DESCRIPTION

To test if the nuevo sol is a commodity currency, this study follows Chen and Rogoff (2003) and Cashin et al (2004), who specify the real effective exchange rate as a function only of the real price of commodities. Given Peru's reliance on commodity exports, in particular metals² such as copper and gold, the hypothesis of commodity currency expects Peru's real effective exchange to be driven primarily by the real price of export commodities. Hence, the regression model takes the following log-linear form:

$$(1) \quad LREER_t = \alpha_0 + \alpha_1 LRP_COM_t + \mu_t$$

Where,

REER = the real effective exchange rate index, which is a trade-weighted and exchange-rate-adjusted ratio of domestic to foreign prices; an increase in the REER is an appreciation. For the robustness exercise, the bilateral real exchange rate index (RER) vis-à-vis the US dollar is also used. The source of REER data is IMF's Information Notice System (INS) database and the RER is constructed using data on the bilateral exchange rate and prices from the IMF's International Financial Statistics (IFS) database.

RP_COM = the real price of export commodities, constructed as the weighted average world price indices of copper, gold, lead and zinc (Peru's major export metals) deflated by the manufacturing export unit value index (MUVI) of advanced economies. Metal price indices are obtained from the IFS database and the MUVI is from the IMF's World Economic Outlook (WEO) database.

μ = stochastic error term.

L = Natural logarithm transformation operator

t = time index.

² Metal exports represent about 55 percent of Peru's total export receipts..

The nuevo sol would be regarded as a commodity currency if α_1 is positive and statistically significant.

To identify the drivers of the equilibrium real effective exchange rate more generally, equation (1) is modified by including the remaining fundamentals and is re-specified as:

$$(2) \quad LREER_t = \beta_0 + \beta_1 * LRP_COM_t + \beta_2 * LPROD_t + \beta_3 * LGCN_t + \beta_4 * LNFL_t + \varepsilon_t$$

Where,

- **PROD** = the relative productivity. The economy-wide labor productivity of Peru relative to a trade-weighted average labor productivity of trading partner countries is used since data on sectoral productivity is not available. The implicit assumption is that productivity growth is likely to be biased in favor of the tradable sector, meaning that a country with high growth of overall productivity will also exhibit higher productivity growth in the tradable sector relative to that of the non-tradable sector. Source of data is Haver.
- **GCN** = the primary current public sector consumption (spending on wages and salaries and goods and services) as a ratio of GDP of Peru relative to that of trading partner countries. Only U.S. data is used in the denominator as consistent time series data is not available for most other trading partner countries such as China, Brazil and Chile. Sources of data are the Central Reserve Bank of Peru (BCRP) and the U.S. Bureau of Economic Analysis (BEA).
- **NFL** = the stock of net foreign liability at end of previous period as a ratio of previous period's total external trade in goods and services. As alternatives, NFL as a ratio of GDP and the cumulative current account balance (as a ratio trade and GDP) are explored. Source of data is the BCRP.
- ε = stochastic error term.
- All other terms are as defined above

The sample covers quarterly data for the period 1992–2013. The year 1992 was chosen as the beginning of the sample period to avoid potential structural shifts in the real exchange rate data due to changes in currency prior to 1992 and major stabilization efforts realized since then. Peru's current currency, the nuevo sol, was introduced and has been in use since July 1991. For robustness exercise, however, annual data for the sample period 1970–2013 and monthly data for the sample period 1992–2013 were also used.

Descriptive analysis of the data shows that Peru's real effective exchange rate is strongly correlated with the relative productivity and the relative government consumption. On the other hand, the real effective exchange rate does not seem to have a discernible correlation

with the real commodity price index and its correlation with the net foreign liability appears to shift from positive prior to 2007 to negative since 2007 (Appendix Figure).

IV. ESTIMATION METHOD AND RESULTS

A. Estimation method

Graphical inspection of data shows that the real effective exchange rate does not seem to exhibit a stationary process as there is a visual evidence of drift in the data (Figure 1a). The first difference of the real exchange rate, however, clearly portrays a stationary process (Figure 1b). This observation is supported by the results of formal unit root tests, which show that Peru's real effective exchange rate follows an I(1) process (Appendix Table 1). Unit root tests for the fundamentals also shows that they are all integrated of order one (Appendix Table 1), implying that the right approach for estimating the real effective exchange rate equation is a cointegration analysis. Hence, the Johansen cointegration method is used to test and estimate cointegration relationships between the REER and the fundamentals. Alternative estimation methods, including the Dynamic OLS (DOLS), the Fully Modified OLS (FMOLS), and the Two-Stage Least Squares (2SLS) methods, are also explored to test the robustness of the results to changes in estimation methodology.

Figure 1. Peru: Real Effective Exchange Rate (in logarithm)

Source: IMF and Author's calculations.

B. Is the nuevo sol a commodity currency?

i) The results

The estimated results below suggest that the real price index of commodities does not explain the behavior of the REER (the number in parenthesis is the t-value).

$$(3) \quad LREER_t = 4.55 + 0.02 * LRP_COM_t \\ (0.793)$$

Although Johansen's Trace and Maximum Eigenvalue tests indicate the presence of cointegration at 10 percent level (Appendix Table 2a), the estimated coefficient on LRP_COM is very small and not statistically significant, ruling out the null hypothesis of a commodity currency. The result is robust to changes in the definition of the real exchange rate (using the RER instead of the REER) and the RP_COM (using the real price of copper and the terms of trade in place of RP_COM), data frequency (using monthly and annual data), estimation method, and sample coverage (Table 1). In all cases, the coefficients are positive as expected, but not statistically significant.

Table 1. Peru: The Real Exchange Rate and Commodity Price: Alternative Specifications

Alternative specification	Coefficient	T-value
Dynamic OLS	0.03	1.21
Fully Modified OLS	0.02	0.43
RER as dependent variable	0.05	0.87
Real price of copper	0.02	0.73
Terms of trade	0.04	0.41
Monthly data: 1992–2013	0.03	1.17
Annual data: 1970–2013	0.01	0.11

The test for linear cointegration in the annual sample yielded no cointegration with coefficients sensitive to changes in specification. Since this might be due to potential structural breaks (regime shifts) as the Peruvian economy underwent through significant turbulences (including hyperinflation and changes in currency) in the 1980s, Gregory-Hansen cointegration test with a regime shift was used to test for evidence of a non-linear cointegration between the REER and RP_COM. The result shows evidence of non-linear cointegration with a regime shift in 1987 at 10 percent level (Appendix Table 3a). Following this result, a dummy was created for this structural shift and the non-linear cointegration relationship was estimated using FMOLS with LRP_COM and LRP_COM interacted with a dummy for a structural shift on the right hand side. The estimated coefficients were -0.26 for

LRP_COM and 0.27 for LRP_COM interacted with a dummy with a net elasticity of 0.01 after the structural shift, i.e. for the period 1987–2013, which is comparable to the sample period of the monthly and quarterly frequency data. Both coefficients were statistically significant, but Wald restriction test for the sum of the coefficients equals zero could not be rejected at any level of significance (Appendix Table 4c).

ii) Possible explanations for why the nuevo sol may not be a commodity currency

While most similar studies on other commodity dependent economies find evidence of commodity currency, Peru was one of the few countries with no such evidence in Cashin et al (2004) as well (Appendix Table 5). The absence of a statistically significant long run relationship between export commodity prices and the real effective exchange rate in an economy that relies heavily for exports on commodities, and that faced significant positive commodity price shocks in the study period, is somewhat puzzling. Potential factors that could have weakened the statistical relationship between the commodity prices and the real effective exchange rate may include large profit repatriation and active foreign exchange intervention.

(i) Profit repatriation: Despite significant price increases for its exports, Peru has run current account deficits during most of the past decade as large profit repatriations more than offset trade surpluses (Figure 2). The mining sector in Peru is operated by the private sector, mostly owned by non-residents. As a result, most of the profit from the sector is repatriated. During 2003–13, the time identified by Adler and Magud (2013) as the commodity income windfall period, profit repatriation from Peru amounted to about 6 percent of GDP a year on average. This might have weakened the statistical relationship between the commodity prices and the real effective exchange rate since a large part of the commodity price shock might have been leaked as profit repatriation without having a significant impact on domestic demand. It is true that a large part of the repatriated profit has been reinvested in Peru in the mining sector, but the investments are mostly on imported machineries with limited impact on domestic demand.

Figure 2. Peru: Real Price of Commodities, Profit Repatriation, and Current Account Balance

Source: BCRP and author's estimations.

(ii) **Active FX intervention:** Peru's central bank intervenes actively in the forex market with a stated objective of limiting exchange rate volatility to contain the risks of financial dollarization. Empirical evidence shows that the BCRP's forex interventions are successful in containing exchange rate volatility (Tashu, 2014). On the other hand, Peru has one of the lowest and most stable rates of inflation in the region, thanks to an inflation targeting framework which has successfully anchored inflation expectations (Armas and Grippa, 2005; Armas et al 2014)³. As a result, Peru's real exchange rate is the most stable among financially open large Latin American economies (Figure 3).

³ While the inflation targeting framework was introduced in 2002, the monetary targeting framework, which was in place prior to 2002, is also credited to have reduced and stabilized inflation from the 1980s hyperinflation.

Figure 3. Real Effective Exchange Rate Indices in Selected Latin American Economies¹
(2010=100)

Sources: IMF and author's calculations.

¹Numbers in parenthesis in front of country names refer to standard deviations of the REER.

A sustained sterilized forex intervention⁴ in an inflation targeting regime appears to have weakened the impact of commodity prices on the real exchange rate. To illustrate this, consider a positive commodity price shock. In an inflation targeting regime, the central bank could prevent the inflationary pressure from the commodity windfall income by increasing its policy rate, which in turn can lead to an increase in capital inflows. In a freely floating exchange rate regime, the capital inflows would have appreciated the nominal, and hence the real, exchange rate. The BCRP's sterilized forex intervention has, however, limited the impacts of capital inflows on the exchange rate, effectively insulating the real exchange rate from the impact of commodity price shocks.

To test the hypothesis that large profit repatriations and the central bank's forex interventions could have insulated the REER from the impact of commodity prices, consider a specification where the REER depends on the commodity prices, profit repatriation in

⁴ Complementary fiscal policy and the use of reserve requirements have helped the BCRP sustain its sterilized forex interventions without compromising the health of its balance sheet. For instances, about 37½ percent and 34½ percent of the forex intervention in 2013 was sterilized by public sector deposits and reserve requirements, respectively, and only about 11½ percent of the intervention was sterilized through central bank instruments (Rossini et al, 2014). In this regard, the positive commodity price shock, which increased tax revenues from the mineral sector, has helped the Treasury to provide support to the central bank's sterilization effort.

percent of GDP (PREP), and net international reserves in percent of GDP (NIR) as a proxy for forex intervention⁵.

$$(4) \quad LREER_t = \theta_0 + \theta_1 * LRP_COM_t + \theta_2 * LPREP_t + \theta_3 * LNIR_t + \epsilon_t$$

Profit repatriation should lead to a depreciation of the nominal, and hence the real, exchange rate because it increases demand for foreign exchange. As a result, $\theta_2 < 0$. The NIR is also expected to have a negative relationship with the real exchange rate as an increase in the NIR (forex purchases by the central bank) and a decrease in NIR (forex sales by the central bank) should lead to a depreciation and appreciation of the national currency, respectively, if successful. Hence, $\theta_3 < 0$.

Since changes in the commodity prices can also affect profit repatriation and net international reserves, we can specify the following equations:

$$(5) \quad LPREP_t = \gamma_0 + \gamma_1 * LRP_COM_t + \varphi_t$$

$$(6) \quad LNIR_t = \delta_0 + \delta_1 * LRP_COM_t + \tau_t$$

From (4), the impact of commodity prices on the REER if we were to hold PREP and NIR constant is θ_1 . In reality, however, both PREP and NIR change when commodity prices change. Firms' profit increases as commodity prices increase, implying $\gamma_1 > 0$, and a positive commodity price shock prompts central bank intervention in the forex market and hence an increase in the NIR, implying $\delta_1 > 0$. As a result, the net impact of commodity prices on the REER is given by $(\theta_1 + \theta_2 * \gamma_1 + \theta_3 * \delta_1)$, and could be zero, negative or positive depending on the relative size of the individual coefficients.

Estimation of equations (4)–(6) using the Johansen cointegration method⁶ yields the following results:

⁵ The NIR used here excludes valuation effects so that changes in NIR reflect mostly of forex interventions and other measures aimed at containing exchange rate volatility such as changes in reserve requirements on foreign currency liabilities.

⁶ All of the variables have unit root (Appendix Table 1). The Augmented-Dickey-Fuller (ADF) test seems to suggest that LNIR is I(0) when constant or constant and trend are added. But the ADF test is known to have low power; i.e., has the tendency to reject the null hypothesis of I(1) too often when it is true. The more efficient unit root test, the Dickey-Fuller GLS (DF-GLS) test, however, accepts the null hypothesis at all levels of significance, suggesting that the NIR is I(1). Johansen's Trace and Maximum Eigenvalue cointegration tests show the presence of a statistically significant cointegration vector among the variables in each of the three equations.

$$(7) \quad LREER_t = 4.22 + 0.49 * LRP_COM_t - 0.16 * LPREP_t - 0.56 * LNIR_t$$

(3.63) (-1.79) (-4.89)

$$(8) \quad PREP_t = -3.87 + 1.01 * LRP_COM_t$$

(5.53)

$$(9) \quad LNIR_t = 0.38 + 0.55 * LRP_COM_t$$

(5.52)

The results show that all of the coefficients have the expected sign and are statistically significant at standard levels of significance. Furthermore, the estimate for the net impact of the commodity prices ($\theta_1 + \theta_2 * \gamma_1 + \theta_3 * \delta_1$), equals 0.01, which is very low and virtually the same as the estimated coefficient obtained when the real effective exchange rate is regressed only on the commodity prices (equation (3)).

Thus, the empirical evidence supports the hypothesis that the commodity price shock has been absorbed mostly by large profit repatriations and a sustained forex intervention, weakening the net impact on the real effective exchange rate. The impact of commodity prices on the real effective exchange rate, if we were to hold profit repatriation constant and assume no forex intervention, would have been statistically significant with an estimated elasticity of about 0.5. In reality, however, changes in commodity prices have statistically significant positive impact on profit repatriation and central bank intervention, which in turn affect the real effective exchange rate negatively, neutralizing the initial impact of the commodity prices on the real effective exchange rate.

C. Identifying the drivers of the equilibrium real exchange rate

The search for a cointegrating vector between the REER and fundamentals involved an algorithm, which: (i) discards models that do not have a statistically significant vector; (ii) eliminates variables which do not have coefficients with theoretically expected sign or whose inclusion changes the signs of other variables; (iii) discards models which do not have a statistically significant error correction term with negative sign; and (iv) maximizes the R-square of the ECM. The net foreign liability was dropped from the chosen model, following this algorithm, similar to the results of other studies, including Montiel (2007) and Coudart et al (2011). Test for cointegration among the remaining variables shows a single cointegrating vector at 10 percent significant level (Appendix Table 2b), which after normalizing for the coefficient of LREER, takes the following form:

$$(10) \quad LREER_t = 4.74 + 0.03 * LRP_COM_t + 0.36 * LPROD_t + 0.37 * LGCN_t$$

(1.48) (2.97) (4.35)

Where numbers in parenthesis refer to t-values.

While all of the fundamentals in equation (10) have the expected signs on their coefficients, the real price of commodities is not statistically significant as is the case in equation (3). Tests for cointegration restrictions show that LRP_COM is not important for the cointegrating vector (Appendix Table 2c). As a result, equation (10) is re-estimated without LRP_COM and the resulting cointegration vector, which becomes statistically significant at 1 percent level (Appendix Table 2d), and the short-run dynamic equation are shown in equations (11) and (12), respectively:

$$\begin{aligned}
 (11) \quad LREER_t &= 4.90 + 0.48 * LPROD_t + 0.39 * LGCN_t \\
 &\quad (3.57) \quad (4.32) \\
 (12) \quad DLREER_t &= 0.0001 - 0.13 * ECM_{t-1} + 0.22 * DLREER_{t-1} \\
 &\quad (0.05) \quad (-3.02) \quad (2.33) \\
 &\quad + 0.45 * DLPROD_{t-1} - 0.09 * DLGCM_{t-1} \\
 &\quad (3.60) \quad (-2.92)
 \end{aligned}$$

Where, D-stands for the first difference, the subscript (-1) refers to the first lag, and ECM stands for the error correction term, which is the error term of equation (11). Numbers in parenthesis are t-values.

Accordingly, relative productivity and government consumption are the main drivers of the equilibrium real effective exchange rate in Peru. The coefficient on the error correction term in the dynamic equation is -0.13 and is statistically significant at 1 percent implying that about 13 percent of deviations of the real exchange rate from the long run equilibrium would be corrected after one quarter. The half-life of a shock to the REER, calculated as $\log(0.5)/\log(1-0.13)$, is estimated at about 5 quarters, which is consistent with the results of other empirical studies. Both productivity and government consumption are also significant in the short run dynamic model (equation (12)), the latter with an unexpected negative sign.

The above result is robust to changes in specifications (Table 2). The exception is when annual data for 1970–2013 is used, which show a statistically significant RP_COM, but the elasticity remains very small (0.03)⁷.

⁷ The results for the annual data are obtained following the procedure described above; i.e. testing for cointegration with regime shift using Gregory-Hansen's test and estimating the long-run relationship using non-linear FMOLS (Appendix Tables 3b, 4b and 4c). In this case, the break was identified as 1988/89.

Table 2. Peru: The Real Exchange Rate and Fundamentals: Alternative Specifications ^{1/}

Alternative Specification	LRP_COM	LPROD	LGCN
Two-stage Least Squares (using first lags as instruments)	0.01 (0.52)	0.43 (8.59)	0.14 (2.09)
Dynamic OLS	0.02 (0.95)	0.36 (3.63)	0.15 (1.95)
Fully Modified OLS	0.01 (0.83)	0.36 (4.20)	0.11 (1.71)
RER as dependent variable ^{2/}	...	0.92 (3.32)	0.41 (2.87)
Real price of copper	0.02 (1.05)	0.40 (3.08)	0.41 (4.38)
Terms of trade	0.05 (0.65)	0.43 (3.12)	0.41 (4.22)
Annual data: 1970-2013 ^{3/}	0.03 (2.95)	0.19 (9.26)	0.19 (8.62)

^{1/} Numbers in parenthesis are t-values.

^{2/} RP_COM is dropped from the bilateral RER model as it carries theoretically-wrong sign.

^{3/} Net foreign liability also becomes significant with theoretically-expected negative sign and elasticity of 0.06. Trade openness index, which was not included in the quarterly data since Peru liberalized its external trade in 1991, is also included in the annual sample (Appendix Tables 4b and 4c).

D. Is the real effective exchange rate misaligned?

While a proper estimation of the equilibrium real exchange rate requires a multi-country panel regression analysis similar to the IMF's external balance assessment (Phillips et al, 2013), the estimated long-run relationship between the REER and statistically significant fundamentals is used to estimate the notional path of the equilibrium REER. The idea is to evaluate how much the actual real effective exchange rate is aligned with the path of the real effective exchange rate predicted by estimated long-run cointegration relationship (equation (11)) and the values of statistically significant fundamentals. In theory, the equilibrium real effective exchange rate is the value of the real effective exchange rate predicted by the 'sustainable' or 'steady state' values of the fundamentals (Montiel, 2007). Hence, the fundamentals are filtered by the Hodrick-Prescott (HP) filter to remove cyclical components and estimate their sustainable components.

The actual, fitted, and equilibrium REER are presented in Figure 4a along with the estimated misalignment in Figure 4b. The fitted value tracks the actual REER very well, indicating a very good fit to data. As a result, the statistical error of the estimated equilibrium REER is likely to be negligible.

Figure 4. Peru: The Equilibrium Real Effective Exchange Rate

Sources: IMF and author's calculations.

The estimated results show that, over the past decade, Peru's real effective exchange rate appears to have been broadly in line with the fundamentals with the exception of mild misalignments in some years. In particular, the REER was:

- *Mildly undervalued during 2004–07 by 2¼ percent on average:* the REER depreciated about 4 percent during this period, while the equilibrium REER depreciated about 2 percent as the impact of large retrenchments in government consumption (relative to the U.S.) more than offset the impact of improvements in relative productivity (Table 3 and Figure 5).
- *Consistent with the equilibrium REER in 2008.*
- *Mildly overvalued during 2009–13 by about 4¾ percent on average:* possibly because the massive capital inflow, which caused a significant REER appreciation (14 percent), was driven not only by Peru's fundamentals, which justified only 9 percent equilibrium REER appreciation, but also by global push factors. However, a large part of the misalignment, which peaked in the 1st quarter of 2013 at 8¾ percent, was corrected in the second half of 2013, as the nuevo sol depreciated following the U.S. Fed Reserve's announcement of monetary policy tapering. (Table 3 and Figure 5)

It is important to note that this assessment does not necessarily have a normative value as a REER close to its equilibrium level may still reflect distortions in the fundamentals (Phillips et al, 2013). A normative assessment of the equilibrium REER requires making judgments on

the ‘appropriateness’ of the fundamentals from a welfare perspective, which is beyond the scope of this study.

Table 3. Peru: Actual and Estimated
Equilibrium Real Effective Exchange Rate

Year	Actual	Equilibrium	Misalignment
2004	100.8	102.1	-1.3
2005	100.0	101.4	-1.4
2006	98.2	100.8	-2.6
2007	96.5	100.2	-3.7
2008	100.8	100.0	0.7
2009	104.1	100.4	3.7
2010	106.6	101.6	5.0
2011	105.5	103.5	1.9
2012	114.5	106.1	7.9
2013	115.0	109.1	5.4

Figure 5. Peru: Contributions of Fundamentals to Changes in EREER
(Percentage change)

V. CONCLUDING REMARKS

This study conducts a cointegration analysis to test the hypothesis of the commodity currency and identify the drivers of Peru’s equilibrium real exchange rate. The first part of the empirical analysis involves testing the hypothesis of ‘commodity currency’ on the nuevo sol. The results show that the real price index of Peru’s export commodities does not have a statistically significant impact on the real effective exchange rate, suggesting that the nuevo sol is not a commodity currency. This appears puzzling for a country that relies heavily on metal commodities for its exports. The paper shows empirically that large profit repatriation and the BCRP’s active forex intervention could have mitigated the impact of commodity prices on the real effective exchange rate.

The second part of the empirical analysis identifies the main drivers of the equilibrium real exchange rate from a pool of economic fundamentals that include the real price of commodities, Peru’s productivity relative to that of trading partners, Peru’s government consumption relative that of trading partners, and the net foreign liability. The results show that only productivity and government consumption, both relative to that of trading partners, have statistically significant relationships with the real effective exchange rate, suggesting that the equilibrium REER is driven only by these two fundamentals.

The equilibrium real effective exchange rate is estimated based on the cointegrating relationship between the real effective exchange rate and the statistically significant fundamentals. The results show that Peru’s real effective exchange rate is broadly in line with the notional equilibrium level predicted by the ‘sustainable’ values of the fundamentals. The REER was mildly overvaluated in the years following the 2008 global financial crisis, which is not surprising given the surge in capital inflows triggered mostly by easy monetary policy in advanced economies. But the recent depreciation of the REER following the U.S. Fed Reserve announcement of unconventional monetary policy tapering in May 2013 appears to have mostly corrected the overvaluation. This does not necessarily imply that all is well with the level of the real exchange rate from a welfare perspective as the equilibrium

real exchange rate itself could be the result of distortions in the fundamentals (suboptimal levels of government consumption, for instance). Making such a normative assessment requires determining the optimal or ‘welfare maximizing’ levels of the fundamentals, which is beyond the scope of this study.

The results of the study on the equilibrium real exchange rate need to be interpreted only as indicative since a proper exchange rate assessment requires a panel data based analysis, in line with the IMF’s EBA assessment, to deal with technical problems associated with small sample size and potential structural breaks.

APPENDIX TABLES

Table 1. Unit Root Test Results ^{1/ 2/}

Variable		ADF t-statistic			DF-GLS t-statistic		Remarks
		None	Constant and trend		Constant and trend		
			Constant		Constant		
Real effective exchange rate	Level	-0.24	-2.59	-2.44	-1.36	-1.71	I(1)
	Difference (1 st)	-7.51	-7.46	-7.53	-7.01	-7.58	
Real bilateral exchange rate	Level	-0.20	-2.37	-1.70	-1.24	-1.37	I(1)
	Difference (1 st)	-6.93	-6.89	-6.96	-6.73	-7.01	
Real price index of export commodities	Level	0.84	-0.73	-2.13	-0.41	-1.76	I(1)
	Difference (1 st)	-6.75	-6.80	-6.79	-6.84	-6.84	
Real price of copper	Level	0.57	-0.89	-2.54	-0.65	-1.87	I(1)
	Difference (1 st)	-7.01	-7.02	-7.01	-7.06	-7.07	
Terms of trade	Level	0.06	-1.78	-2.41	-1.78	-2.19	I(1)
	Difference (1 st)	-6.38	-6.34	-6.29	-6.21	-6.24	
Relative productivity	Level	-0.57	-0.93	-0.54	-0.91	-0.73	I(1)
	Difference (1 st)	-8.01	-7.98	-7.99	-2.50	-6.19	
Relative government consumption	Level	-1.05	-2.44	-2.51	-0.48	-1.11	I(1)
	Difference (1 st)	-15.08	-15.03	-17.08	-1.67	-3.46	
Net foreign liability ^{3/}	Level	-0.95	-0.65	-1.44	0.53	-1.43	I(1)
	Difference (1 st)	-6.97	-7.36	-7.32	-7.38	-7.33	
Net international reserves ^{4/}	Level	2.50	-4.46	-4.35	0.94	-1.03	I(1)
	Difference (1 st)	-6.34	-6.81	-7.14	-4.53	-5.60	
Profit repatriation ^{4/}	Level	-0.58	-1.50	-2.38	-0.90	-2.51	I(1)
	Difference (1 st)	-12.16	-12.12	-12.10	-11.93	-11.63	
Critical Values							
1%		-2.59	-3.51	-4.07	-2.59	-3.63	
5%		-1.95	-2.90	-3.46	-1.95	-3.07	
10%		-1.61	-2.59	-3.16	-1.61	-2.78	

^{1/} Null Hypothesis is unit root in all cases. The Null Hypothesis is accepted for t-statistics greater than corresponding critical values.

^{2/} All variables are expressed in natural logarithmic form.

^{3/} As a ratio of previous period's total external trade in goods and services.

^{4/} In percent of GDP.

Table 2. Johansen Cointegration Tests between the Real Effective Exchange Rate and the Fundamentals

(a) Cointegration between LREER and LRP_COM

<i>Unrestricted Cointegration Rank Test (Trace)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Trace Statistic	Critical Value	Prob. ^{1/}
None*	0.147	14.960	15.495	0.060
At most 1	0.015	1.304	3.841	0.254
<i>Unrestricted Cointegration Rank Test (Maximum Eigenvalue)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Maximum-Eigen Statistic	Critical Value	Prob. ^{1/}
None*	0.146826	13.6561	14.2646	0.0622
At most 1	0.015048	1.30398	3.841466	0.2535

^{1/} MacKinnon-Haug-Michelis (1999) p-values

*Rejection of the hypothesis at 10% level.

(b) Cointegration among LREER, LRP_COM, LGCN, and LPROD_M

<i>Unrestricted Cointegration Rank Test (Trace)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Trace Statistic	Critical Value	Prob. ^{1/}
None*	0.266075	46.37389	47.85613	0.0684
At most 1	0.120272	19.76994	29.79707	0.4385
At most 2	0.071095	8.749647	15.49471	0.3891
At most 3	0.027603	2.407229	3.841466	0.1208
<i>Unrestricted Cointegration Rank Test (Maximum Eigenvalue)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Maximum-Eigen Statistic	Critical Value	Prob. ^{1/}
None*	0.266075	26.60395	27.58434	0.0663
At most 1	0.120272	11.02029	21.13162	0.6453
At most 2	0.071095	6.342418	14.2646	0.5697
At most 3	0.027603	2.407229	3.841466	0.1208

^{1/} MacKinnon-Haug-Michelis (1999) p-values

*Rejection of the hypothesis at 10% level.

(c) Cointegration restriction tests

Null hypothesis	Restricted log-likelihood	LR Statistic	Degrees of Freedom	Probability
Coefficient on LRP_COM is zero	650.3344	1.920112	1	0.1658
Coefficient on LPROD is zero **	649.2462	4.096616	1	0.0430
Coefficient on LGCN is zero***	645.7832	11.02264	1	0.0009

** Rejection of the hypothesis at 5% level.

*** Rejection of the hypothesis at 1% level.

(d) Cointegration among LREER, LGCN, and LPROD_M

Hypothesized no. of CE(s)	Eigenvalue	Trace Statistic	Critical Value	Prob. ^{1/}
None ***	0.236197	37.57606	29.79707	0.0052
At most 1	0.103207	14.40381	15.49471	0.0725
At most 2 **	0.056874	5.035806	3.841466	0.0248
<i>Unrestricted Cointegration Rank Test (Maximum Eigenvalue)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Maximum-Eigen Statistic	Critical Value	Prob. ^{1/}
None **	0.236197	23.17225	21.13162	0.0255
At most 1	0.103207	9.368004	14.2646	0.2568
At most 2 **	0.056874	5.035806	3.841466	0.0248

^{1/} MacKinnon-Haug-Michelis (1999) p-values

** Rejection of the hypothesis at 5% level.

*** Rejection of the hypothesis at 1% level.

Table 2. Johansen Cointegration Tests between the Real Effective Exchange Rate and the Fundamentals (concluded)

(e) LREER, LRP_COM, LPROFIT, and LNIR

<i>Unrestricted Cointegration Rank Test (Trace)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Trace Statistic	Critical Value	Prob. ^{1/}
None **	0.3317	54.1336	47.8561	0.0115
At most 1	0.1118	20.2804	29.7971	0.4040
At most 2	0.0752	10.3257	15.4947	0.2565
At most 3*	0.0438	3.7582	3.8415	0.0525
<i>Unrestricted Cointegration Rank Test (Maximum Eigenvalue)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Maximum- Eigen Statistic	Critical Value	Prob. ^{1/}
None ***	0.331698	33.85326	27.58434	0.0069
At most 1	0.111755	9.954619	21.13162	0.7489
At most 2	0.075207	6.567558	14.2646	0.5415
At most 3*	0.043754	3.758178	3.841466	0.0525

^{1/} MacKinnon-Haug-Michelis (1999) p-values

* Denotes rejection of the hypothesis at 10% level.

** Denotes rejection of the hypothesis at 5% level.

*** Denotes rejection of the hypothesis at 1% level.

(f) LNIR and LRP_COM

<i>Unrestricted Cointegration Rank Test (Trace)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Trace Statistic	Critical Value	Prob. ^{1/}
None ***	0.247573	24.18814	15.49471	0.0019
At most 1	0.003496	0.294206	3.841466	0.5875
<i>Unrestricted Cointegration Rank Test (Maximum Eigenvalue)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Maximum- Eigen Statistic	Critical Value	Prob. ^{1/}
None ***	0.247573	23.89393	14.2646	0.0011
At most 1	0.003496	0.294206	3.841466	0.5875

^{1/} MacKinnon-Haug-Michelis (1999) p-values

*** Denotes rejection of the hypothesis at 1% level.

(g) LPROFIT and LRP_COM

<i>Unrestricted Cointegration Rank Test (Trace)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Trace Statistic	Critical Value	Prob. ^{1/}
None **	0.155422	16.85422	15.49471	0.031
At most 1	0.031229	2.665094	3.841466	0.1026
<i>Unrestricted Cointegration Rank Test (Maximum Eigenvalue)</i>				
Hypothesized no. of CE(s)	Eigenvalue	Maximum- Eigen Statistic	Critical Value	Prob. ^{1/}
None*	0.155422	14.18913	14.2646	0.0514
At most 1	0.031229	2.665094	3.841466	0.1026

^{1/} MacKinnon-Haug-Michelis (1999) p-values

* Denotes rejection of the hypothesis at 10 level.

** Denotes rejection of the hypothesis at 5 level.

Table 3. Gregory-Hansen Test for Cointegration with Regime
Shift: annual sample (1970-2013)^{1/}

(a) LREER and LRP_COM

	Test		Asymptotic critical values		
	statistic	Shift year	1%	5%	10%
ADF	-4.70*	1987	-5.47	-4.95	-4.68
Z _t	-4.75*	1987	-5.47	-4.95	-4.68
Z _a	-30.34	1987	-57.17	-47.04	-41.85

(b) LREER and All Fundamentals ^{2/}

	Test		Asymptotic critical values		
	statistic	Shift year	1%	5%	10%
ADF	-7.08***	1988	-6.92	-6.41	-6.17
Z _t	-6.24*	1989	-6.92	-6.41	-6.17
Z _a	-30.34	1989	-90.35	-78.52	-75.56

^{1/} The null hypothesis is 'no cointegration'.

^{2/} Includes LRP_COM, LPROD, LGCN and LNFL.

*Null hypothesis is rejected at 10% significance level.

***Null hypothesis is rejected at 1% significance level.

Table 4. Estimating Non-linear Cointegrations using the FMOLS Method: annual sample (1970-2013)

(a) LREER and LRP_COM

$$\text{LREER} = a(1) * \text{LRP_COM} + a(2) * \text{LRP_COM} \times \text{RS1987} + a(3)$$

Coefficient ^{1/}	Coefficient	Standard error	Probability
a(1)	-0.26	0.12	0.0349
a(2)	0.27	0.02	0.0000
a(3)	4.59	0.54	0.0000

(b) LREER and All Fundamentals

$$\text{LREER} =$$

$$b(1) * \text{LRP_COM} + b(2) * \text{LRP_COM} \times \text{RS1988} + b(3) * \text{LGCN} + b(4) * \text{LGCN} \times \text{RS1988} + b(5) * \text{LPROD} + b(6) * \text{LPROD} \times \text{RS1988} + b(7) * \text{LNFL} + b(8) * \text{TRADE_OPEN} + b(9)$$

Variable ^{2/}	Coefficient	Standard error	Probability
b(1)	-0.16	0.01	0.0000
b(2)	0.19	0.00	0.0000
b(3)	-0.44	0.03	0.0000
b(4)	0.63	0.04	0.0000
b(5)	-0.76	0.04	0.0000
b(6)	0.95	0.04	0.0000
b(7) ^{3/}	-0.06	0.01	0.0000
b(8) ^{3/ 4/}	0.52	0.01	0.0000
b(9)	4.01	0.04	0.0000

(c) Wald coefficient restriction tests

Null hypothesis	value	t-statistic	Probability
a(1)+a(2)=0	0.01	0.11	0.9100
b(1)+b(2)=0	0.03	2.95	0.0057
b(3)+b(4)=0	0.19	9.26	0.0000
b(5)+b(6)=0	0.19	8.62	0.0000

^{1/} RS1987 refers to dummy for regime shift in 1987, identified by the Gregory-Hansen test (Appendix Table 3a).

^{2/} RS1988 refers to dummy for regime shift in 1988, identified by the Gregory-Hansen test (Appendix Table 3b).

^{3/} LNFL and TRADE_OPEN (dummy for trade openness) show no change in the sign of their coefficients when interacted with RS1988. As a result, they are included without interactions.

^{4/} TRADE_OPEN was not included in the cointegration test in Appendix Table 3b since the Gregory-Hansen test does not allow for more than four right hand side variables and dummy variables.

Table 5. Empirical Evidence on Commodity Currency

Author/s (year)	Country/ies	Sample	Method	Elasticity on commodity prices	Definition of commodity prices
Chen and Rogoff (2003)	Australia, Canada, New Zealand	Quarterly: year varies	Time Series cointegration	Australia (0.4), Canada (0.4), and New Zealand (0.6)	Real commodity prices
Cashin et al (2004)	58 commodity exporting countries, including Peru	Monthly: 1980-2002	Time Series cointegration	Median=0.4. TOT not important for Peru.	Real commodity prices
Ferreira and Salas (2006)	Peru	Quarterly: 1980-2005	Time series cointegration	0.3	TOT
Montiel (2007)	Argentina, Bolivia, Brazil, Chile, Paraguay, Uruguay	Annual: 1969-2005	Time series cointegration	TOT important only for Argentina (1.7), Bolivia (0.6), and Uruguay(0.6)	TOT
Iossifov and Loukoianova (2007)	Ghana	Quarterly: 1984-2006	Time series cointegration	0.4	Real commodity prices
Astorga (2012)	Argentina, Brazil, Chile, Colombia, Mexico, Venezuela	Annual: 1900-2000	Time series cointegration	Argentina (0.4), Brazil (0.2), Chile (0.1), Colombia (0.4), Mexico (not significant), Venezuela (0.1)	TOT
Coudert et al (2011)	52 commodity exporters	Annual: 1980-2007	Panel cointegration	0.4	Real commodity prices
Boudart (2012)	42 commodity dependent countries	Monthly: 1980-2009	Panel cointegration	0.2	Real commodity prices
Ricci et al (2013)	48 industrial and emerging countries	Annual: 1980-2004	Panel cointegration	Advanced countries (0.8) Emerging markets (0.5)	Real commodity prices
Phillips et al (2013)	40 advanced and emerging countries	Annual: 1990-2010	Panel OLS(fixed effect)	0.1	Real commodity prices

APPENDIX FIGURE

Peru: The Real Effective Exchange Rate and the Fundamentals

Source: BCRP, BEA, Haver, IFS, INS, WEO, and author's calculations.

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